

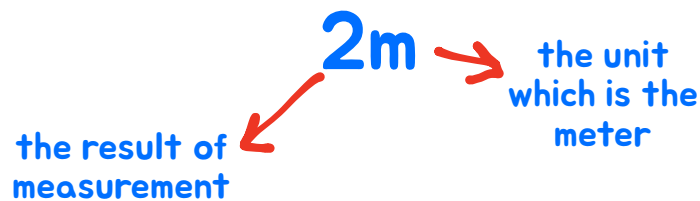
# Chapter 1

## sections 1.5 & 1.6 & 1.8

### Sec 1.5

## Units, Standards, and the SI system

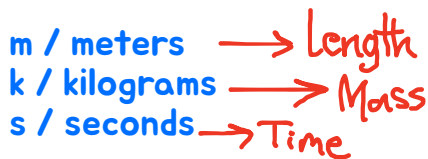
When we measure the height of a table we may write :-



There are three main units that we use and they are :-



We usually use the "mks" system which is referred to :-



it's called System International in French, but we say it in English International System

there is also other basic units like :-

electric current : A "ampere"  
temperature : K "Kelvin"  
amount of substance : mole  
luminous intensity : cd "candela"

the "cgs" system is referred to :-

c / centimeters  
g / grams  
s / seconds

## Sec 1.6

# Converting Units

it is easy to change from mks to cgs and the opposite for example :-

$$1\text{m} = 100\text{cm} \quad , \quad 1\text{kg} = 1000 \text{ grams}$$

there is also something called ( conversion factor ) example :-

$$9\text{m} = ?\text{cm} / 9\text{m} \times 1 = \cancel{9\text{m}} \times \frac{100\text{cm}}{\cancel{\text{m}}}$$

$$9\text{m} = 900\text{cm}$$

another example :-

$$1\text{km} = 1000\text{cm} \text{ :- } 3\text{km} = ?\text{cm} / \cancel{3\text{km}} = \frac{1000\text{cm} \times 3}{\cancel{\text{km}}} \rightarrow 3 = 3000 \text{ cm}$$

consider the following :-

velocity	سرعة	m/s	→	L/T	( we express these in the term of :- L,M,T )
acceleration	تسارع	m/s <sup>2</sup>	→	L/T <sup>2</sup>	
density	كثافة	kg/m <sup>3</sup>	→	M/L <sup>3</sup>	

also, momentum (  $p = mv$  ) , force (  $F = ma$  ) are expressed in terms of L,M,T

**example:- show that force which has units of (newton) can be expressed in terms of the base quantities L,M,T**

$$F = m \overset{\text{acceleration}}{a}$$

$\swarrow$  the unit of force is the newton (N)  
 ماسي

$$1\text{N} = 1\text{kg} \cdot 1\text{m/s}^2 = \text{M} \cdot \text{L/T}^2$$

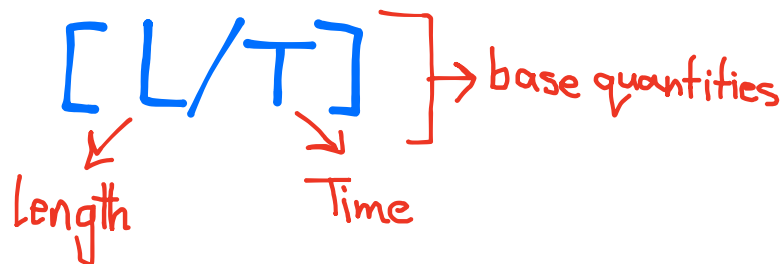
therefore the newton is a derived quantity , since we can express it in terms of combination of the base unites

## Sec 1.8

### Dimension and Dimensional Analysis

Dimension of velocity (v):-

base quantities are used to express velocity



it means that velocity is measured in units of :-

m/s or cm/s or km/h... etc

Length/time

### Dimensional Analysis :-

$$xy + z = 2$$

each of (xy, z, 2) are terms they may have different values but each of them are a term

\*this question is important ( Is this equation dimensionally correct? )

it should be "not the same but all of them should equal each other" :

$$[L/T] = [L/T] + [L/T]$$

to be dimensionally correct \*it might not be physically correct\*

but, if it's otherwise then it is both dimensionally and physically incorrect

**Question:** what are the dimensions of force?

**Answer:** \*remember\*  $F = ma$   
 dimensions of force are  $\rightarrow [M \frac{L}{T^2}]$   
 mass  $\rightarrow$  Length  $\rightarrow$  time  $\rightarrow$

**Example:** is the relation  $V_f = V_i + at^2$  incorrect?

**Answer:** by using the dimensional analysis the dimensions of V is  $[L/T]$  and dimensions of time is  $[T]$

$$[\frac{L}{T}] \stackrel{?}{=} [\frac{L}{T}] + [\frac{L}{T^3}] [T^2]$$

$$[\frac{L}{T}] = [\frac{L}{T}] + [L]$$

same dimensions
different dimension

so this relation is dimensionally and physically incorrect

**Consider:-**  $V_f = V_i + \frac{1}{2}at$   
 give the dimensional analysis:-

$$[\frac{L}{T}] \stackrel{?}{=} [\frac{L}{T}] + [\frac{L}{T} \times T] =$$

$$[\frac{L}{T}] = [\frac{L}{T}] + [\frac{L}{T}] \rightarrow \text{All terms have the same dimensions}$$

**Remember:-**

it can be:-

dimensionally & physically correct

only dimensionally correct

dimensionally & physically

incorrect

$V_f = V_i + at$   
 0- physically correct  
 0- dimensionally correct

it is dimensionally correct but, physically incorrect

## Solving problems and add notes:-

17. (II) Determine the conversion factor between (a) km/h and mi/h, (b) m/s and ft/s, and (c) km/h and m/s.

we will change km/h to mi/h

Note: 1km = 1000m , 0.621mi = 1km , 1h = 3600s

conversion factor from km/h to mi/h :

$$\frac{1\text{km}}{\text{h}} = 1 \frac{\cancel{\text{km}}}{\text{h}} \times \left( \frac{0.621\text{mi}}{\cancel{\text{km}}} \right) = 0.621 \text{ mi/h}$$

$$\therefore 1 \frac{\text{km}}{\text{h}} = 0.621 \text{ mi/h} \rightarrow 1 = \frac{0.621 \text{ mi/h}}{\text{km/h}}$$

for example:- what is 40 km/h in mi/h?

$$40 \text{ km/h} = 40 \frac{\cancel{\text{km}}}{\cancel{\text{h}}} \times 0.621 \frac{\text{mi}}{\text{h}} = 40 \times 0.621 \frac{\text{mi}}{\text{h}} = \underline{24.84 \text{ mi/h}}$$

km/h and m/s :-

$$1\text{km/h} = 1 \frac{\cancel{\text{km}}}{\cancel{\text{h}}} \times (1000\cancel{\text{m}}/\cancel{\text{km}}) \times (\cancel{\text{h}}/3600\text{s})$$

$$1\text{km/h} = 5/18 - \text{m/s} \Rightarrow 1 = 5/18 (\text{m/s}) / (\text{km/h})$$

14. (I) One hectare is defined as  $1,000 * 10^4 \text{ m}^2$ .  
One acre is  $4,356 * 10^4 \text{ ft}^2$ . How many acres are in one hectare?

$$\text{hectare} = 1 \times 10^4 \text{ m}^2$$

$$1\text{ft} = 0.3048\text{m}$$

$$\text{acer} = 4.356 \times 10^4 \text{ ft}^2$$

$$1\text{ft}/0.3048\text{m} = 1$$

$$1 \text{ hectare} = (1 \times 10^4) \left( \frac{\cancel{\text{ft}}}{0.3048\text{m}} \right)^2 \times \left( \frac{\text{acre}}{4.356 \times 10^4 \cancel{\text{ft}^2}} \right) = (1 \times 10^4) \times \frac{1}{0.3048^2} \times \frac{1}{4.356 \times 10^4}$$

$$= 2.471 \text{ acre}$$

21. (II) (a) How many seconds are there in 1.00 year? (b) How many nanoseconds are there in 1.00 year? (c) How many years are there in 1.00 second?

a)  $1 \text{ year} = 1 \times 365 \times 24 \times 60 \times 60 = 3.16 \times 10^7 \text{ s}$   
 $1 \text{ y} = 3.16 \times 10^7 \text{ s} \Rightarrow 3.16 \times 10^7 \text{ s/y} \rightarrow \text{conversion factor}$

b)  $\text{nano} = 10^{-9}$   
 $1 \text{ ns} = 10^{-9} \text{ s} \quad 1 = (10^9 \text{ s/ns})$   
 $1 \text{ y} = 1 \text{ y} \times (3.16 \times 10^7 \text{ s/y}) \times (10^9 \text{ ns/s}) = 3.16 \times 10^{16} \text{ ns}$

c)  $1 \text{ s} = 1 \text{ s} \times (1 \text{ y} / 3.16 \times 10^7 \text{ s}) = 3.165 \times 10^{-8} \text{ y}$

$$1 \text{ s} = \frac{1 \text{ min}}{60 \text{ s}} \times \frac{1 \text{ h}}{60 \text{ min}} \times \frac{1 \text{ day}}{24 \text{ h}} \times \frac{1 \text{ y}}{365 \text{ day}} = \frac{1 \text{ y}}{31536000} = 3.17 \times 10^{-8}$$

$$= 3.17 \times 10^{-8} \text{ y}$$

\*33. (I) What are the dimensions of density, which is mass per volume?

density ( $\rho$ ) = mass / volume

dimensions are :  $[M / L^3]$

\*34. (II) The speed  $v$  of an object is given by the equation  $v = At^3 - Bt$ , where  $t$  refers to time. (a) What are the dimensions of  $A$  and  $B$ ? (b) What are the SI units for the constants  $A$  and  $B$ ?

a & b)

$V = At^3 - Bt$  where ( $t$ ) is time

the equation must be dimensionally correct

$V$  has dimensions of  $L/T$

$$\left[\frac{L}{T}\right] = [A T^3] - [B T]$$

↪ must have the dimensions of  $L/T$

↪ must have the dimensions of  $L/T$

$$[A T^3] = \left[\frac{L}{T}\right] \rightarrow \text{dimensions of } A \text{ must be } L/T^3$$

$$[B T] = \left[\frac{L}{T}\right] \rightarrow \text{dimensions of } B \text{ must be } L/T^2$$

48. An angstrom (symbol  $\text{\AA}$ ) is a unit of length, defined as  $10^{-10}$  m, which is on the order of the diameter of an atom. (a) How many nanometers are in 1.0 angstrom? (b) How many femtometers or fermis (the common unit of length in nuclear physics) are in 1.0 angstrom? (c) How many angstroms are in 1.0 m? (d) How many angstroms are in 1.0 light-year (see Problem 18)?

$$\text{Angstrom} = 10^{-10} \text{ m}$$

$$1 \text{\AA} = 10^{-10} \text{ m} \Rightarrow 1 = 10^{-10} \text{ m} / \text{\AA} \quad ] \rightarrow \text{conversion factor}$$

$$1 \text{\AA} = 1 \text{\AA} \times \left( \frac{10^{-10} \text{ m}}{\text{\AA}} \right) \times \left( \frac{10^9 \text{ nm}}{\text{m}} \right) = 10^{-1} \text{ nm}$$

$$10^{-10} \text{ nm} \Rightarrow 1 = \frac{10^{-1} \text{ nm}}{\text{\AA}} = \frac{0.1 \text{ nm}}{\text{\AA}}$$

# Chapter 2

Sec 2.1 & 2.2 & 2.3 & 2.4

## Kinematic in one dimension

It means: moving along in one line

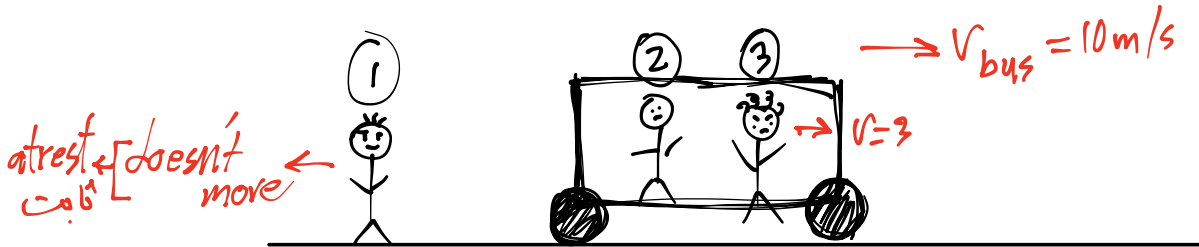
### Sec 2.1 :- Fram of reference إطار الـسناد

\* Velocity is a vector

السرعة عبارة عن متجه

\* Pressure, temperature, mass, speed: they are scalar that has magnitude مقدار قياسي

Describing farm of reference: from each person point view



1 for Person 1 he sees person 2 moves to the right with  $v = 10 \text{ m/s}$  and person 3 moves to the right with  $v = 13 \text{ m/s}$  because  $v_{\text{bus}} + v_3 = 13 \text{ m/s}$

2 for person 2 he sees person 1 moves to the left with  $v = 10 \text{ m/s}$  and sees person 3 moving to the right with  $v = 3 \text{ m/s}$

3 for person 3 he sees person 2 moves to the left with  $v = 3 \text{ m/s}$  and sees person 1 moves to the left with  $v = 13 \text{ m/s}$ .



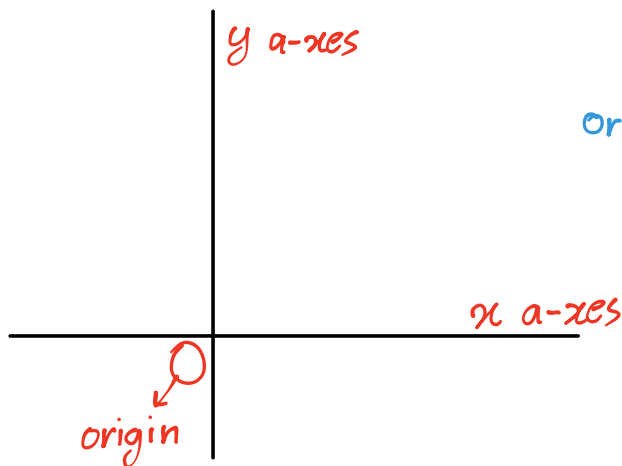
\* Velocity, force, distanced have magnituded and directions  
مقدار      اتجاه

**Note:** every point of view is correct & it depends on the observe of each person.

we use fram of reference to specify velocity in specific view

## What dose fram of referenc consist of?

It dose consists two dimensions the  $x$  and the  $y$  a-axes

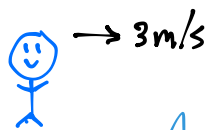


note:- in case 1 the person was representing a fram of reference as an origin poin and give positions with aspect to the origin and measures velocity with aspect of a-axes ( $x$  and  $y$ ).

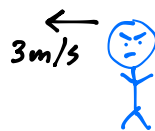
## Sec 2.2 :- Average Velocity

more explanation:-

person 1



person 2



$$A. \text{velocity} = \frac{\text{displasment}}{\text{time}} = m/s$$

Both person 1 & 2 have the same speed & speed gives how fast an object or someone moving

So if we say you have moved a distance of 9m in 3s we define an average speed  $\bar{s}$  as:-  

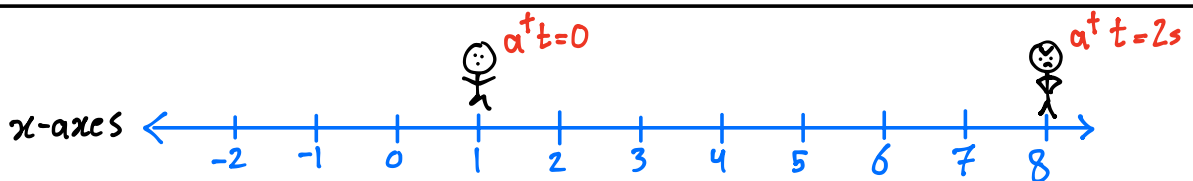
$$\bar{s} = \frac{\text{distance}}{\text{time}} = \frac{9}{3} = 3 \text{ m/s}$$

Q :- what is the difference between speed & velocity?  
 we can say that person 1 moves at  $3 \text{ m/s}$  in the positive x-direction  
 ↳ magnitude                      ↳ direction

\* Note:- the directions will be the same as the displacement in Velocity  
 & the reason that it's vector, because it contains direction as well as magnitude of a moving object.  
 ↳ magnitude                      ↳ الاتجاه

So person 1 /  $v_1 = +3 \text{ m/s}$   
 ↳ direction to the right (along positive x direction)

and person 2 /  $v_2 = -3 \text{ m/s}$   
 ↳ direction to the left (along negative x direction)



\* the person was (at  $x=1 \text{ m}$  at  $t=0 \text{ s}$ )  
 and he moved to ( $x=8 \text{ m}$  at  $t=2 \text{ s}$ )

So we define average velocity as:-

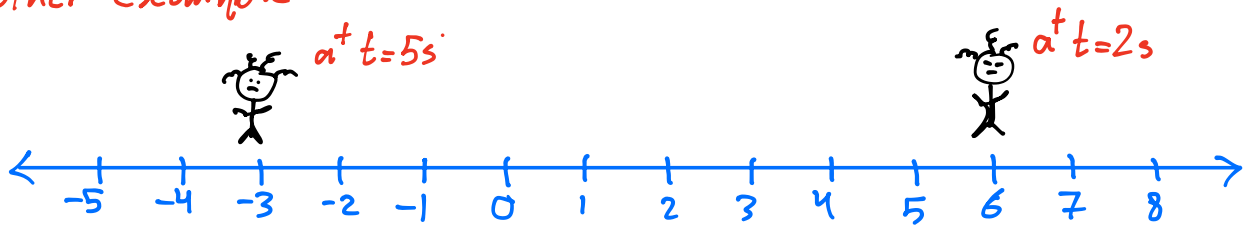
the line means average  $\bar{v} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i}$     i = initial / أولي / ابتدائي    f = final / نهائي

$$\bar{v} = \frac{\Delta \text{displacement}}{\Delta \text{time}}$$

So we can write:-  $\bar{v}_{0-2} = \frac{8-1}{2-0} = \frac{7}{2} = 3.5 \text{ m/s}$

\* Average velocity depends on the change in displacement

another example:-



Q: Find the average velocity of the person over the time interval  $t=2s \rightarrow t=5s$

$$\bar{v}_{2-5} = \frac{-3 - 6}{5 - 2} = \frac{-9}{3} = -3 \text{ m/s} \quad (\text{because } -3 \times 3 = -9)$$

So  $\bar{v}_{2-5} = -3 \text{ m/s}$   
↑ that means that  $\bar{v}$  is along the negative  $x$ -direction

## Sec 2.3 :- Instantaneous Velocity

سرعة لحظية

If we said that we were driving and we looked at the odometer (عداد السرعة) we may read  $50 \text{ km/h}$ . And this's the velocity at a given instant.

\* And we call this instantaneous velocity. Which's given at a particular instant of time.

for example:-

$v = 60 \text{ km/h} \rightarrow$  direction in positive  $x$ -ases

$v = -40 \text{ km/h} \rightarrow$  direction in negative  $x$ -ases

## Sec 2.4 Acceleration

When the velocity of an object changes with time then this object accelerates

\* Acceleration is the change in velocity with time  
التسارع يعتمد على التغير في السرعة وليس السرعة عندها.

Average Acceleration  $\bar{a}$

$$\bar{a} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i} = \text{m/s}^2 \quad \text{[examples:-]}$$

Q\ if the velocity of an object is zero ,  
dose the acceleration have to be zero?

NO , it dose not

$$\begin{array}{l} t_i = 1 \quad v_i = 3 \text{ m/s} \\ t_f = 5 \quad v_f = 10 \text{ m/s} \end{array} \quad \bar{a} = \frac{\Delta v}{\Delta t} = \text{m/s}^2$$

$$\bar{a} = \frac{10 - 3}{5 - 1} = \frac{7}{4} = 1.75 \text{ m/s}^2$$

Find the average acceleration of the car

$$t_i = 2 \text{ s} \quad , \quad v_i = 4 \text{ m/s}$$

$$t_f = 2 + 3 = 5 \text{ s} \quad , \quad v_f = 12 \text{ m/s}$$

$$\bar{a} = \frac{\Delta v}{\Delta t} = \frac{12 - 4}{5 - 2} = \frac{8}{3} \approx 2.7 \text{ m/s}^2$$

# Problems Chapter 2 & Notes

Note:-

$v$	$a$	$\bar{a}$
+	+	+
-	-	-
+	-	deceleration
-	+	deceleration

} تباطؤ

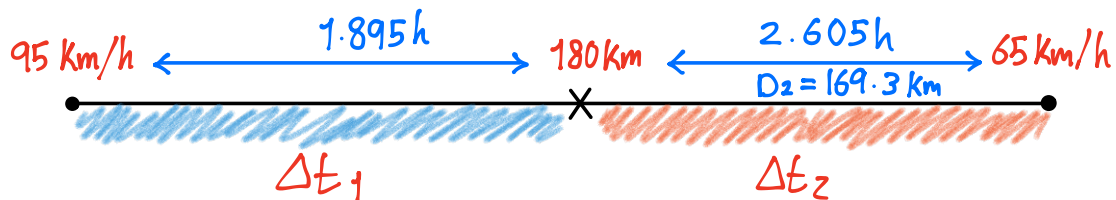
5. (I) A bird can fly 25 km/h. How long does it take to fly 3.5 km? we use the velocity here

$$\bar{v} = \frac{\Delta x}{\Delta t} \Rightarrow \Delta t? \quad \Delta t = \frac{\Delta x}{\bar{v}}, \quad \Delta t = \frac{3.5 \text{ km}}{25 \text{ km/h}} = 0.14 \text{ h}$$

7. (II) You are driving home from school steadily at 95 km/h for 180 km. It then begins to rain and you slow to 65 km/h. You arrive home after driving 4.5 h.

(a) How far is your hometown from school?

(b) What was your average speed?



1  $\bar{v} = \frac{\Delta x}{\Delta t} = \frac{180}{\Delta t} = 95 \Rightarrow \Delta t = \frac{180}{95} = 1.895 \text{ h}$

2  $4.5 - 1.895 = 2.605 \text{ h}$

3  $2.605 \text{ h} \times 65 \text{ km/h} = 169.3 \text{ km}$

4 Average Speed:-

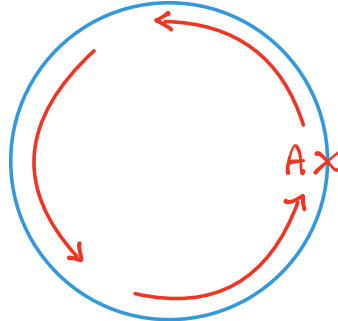
$$\bar{s} = \frac{\text{total distance}}{\text{total time}} = \frac{180 + 169.3}{4.5}$$

$$\bar{s} = 77.6 \text{ km/h}$$

9. (II) A person jogs eight complete laps around a 400m track in a total time of 14.5 min. Calculate

- (a) the average speed.  
 (b) the average velocity, in ms.

a)



one complete (circle) is 400m. in 14.5 min  
 So 8 complete lap =  $8 \times 400 = 3200 \text{ m}$

note:- if the objects returns to the starting point the  $\Delta x = \text{Zero}$

So the average speed is  $\bar{v} = \frac{\text{distance}}{\text{time}} = \frac{3200 \text{ m}}{14.5 \text{ min}} = 220.7 \text{ m/min}$

b) the runner has began from point A and returned to point A  
 So the average velocity is Zero  
 to be sure  $\Delta x = x_f - x_i = 0$

11. (II) A car traveling 95 km/h is 210 m behind a truck traveling 75 km/h. How long will it take the car to reach the truck?



we will use the velocity :-

\* the car have travelled 210 m, so dose the truck, so we can say that the  $d_{\text{car}} = d_{\text{truck}} + 210$   
 Car & the truck have equal distance plus 210 m

$$1 \quad v_c = \frac{\Delta x_c}{\Delta t}, \quad v_t = \frac{\Delta x_t}{\Delta t} \Rightarrow \Delta t = \frac{d_c}{v_c}, \quad \frac{d_c}{v_c}$$

$$2 \quad \frac{d_t + 210}{95} = \frac{d_t}{75}$$

بما معناه :- السيارة تمشي بسرعة 95 كم/س و بينها و بين الشاحنة مسافة 210 م و الشاحنة تمشي بسرعة 75 كم/س. المطلوب هو الزمن اللازم الذي سوف تقطعه السيارة بمسافة 210 م زائد المسافة التي قطعتها الشاحنة وهي تتحرك بسرعة 75 كم/س فتصبح عندي مسافتين (d-car & d-truck) و المسافة المعطاه 210 م

$$3 \quad \therefore 75(dt + 210) = 95 dt$$

$$75 \times 210 + 75 dt = 95 dt \quad = \frac{75 \times 210}{20} = 787.5 \text{ m} \quad dt$$

$$4 \quad \text{now we use } \frac{dt}{v_t} = \Delta t = \frac{787.5 \text{ m}}{75 \text{ km/h} \times \frac{1000 \text{ m}}{\text{km}}} = 10.5 \times 10^{-3} \text{ h} \times \frac{3600 \text{ s}}{\text{h}}$$

$$\Delta t = 37.8 \text{ s}$$

20. (II) At highway speeds, a particular automobile is capable of an acceleration of about  $1.8 \text{ m/s}^2 \rightarrow \alpha$

At this rate, how long does it take to accelerate from  $\overset{V_i}{65 \text{ km/h}}$  to  $\overset{V_f}{120 \text{ km/h}}$ ?

1 using the conversion factor :-

$$65 \text{ km/h} \times \frac{5 \text{ m}}{1000 \text{ m}} \times \frac{\text{h}}{3600 \text{ s}} = 65 \times \frac{5 \text{ m}}{18 \text{ s}} = 18.1 \text{ m/s}$$

$$120 \text{ km/h} \times \frac{5 \text{ m}}{1000 \text{ m}} \times \frac{\text{h}}{3600 \text{ s}} = 120 \times \frac{0.27}{18} = 33.3 \text{ m/s}$$

2 now we use  $\bar{a}$  :-

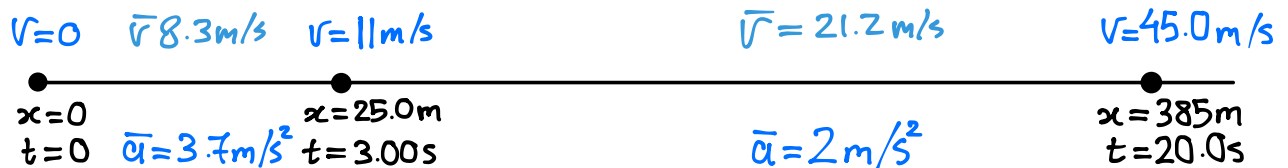
$$\bar{a} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i} = \frac{33.3 - 18.1}{1.8 \text{ m/s}^2} = 8.4 \text{ s}$$

note: the reason that we used conversion factor is that the velocity & acceleration need to be in the same units  $\text{m/s}$  &  $\text{m/s}^2$  or  $\text{km/h}$  &  $\text{km/h}^2$

what if I want to use the  $\text{km/h}$ ,  $\text{km/h}^2$ ?

in the questions that's given speed is velocity until it proven that it's speed

21. (II) A car moving in a straight line starts at  $x = 0$  at  $t = 0$ . It passes the point  $x = 25.0$  m with a speed of  $11.0$  m/s at  $t = 3.00$  s. It passes the point  $x = 385$  m with a speed of  $45.0$  m/s at  $t = 20.0$  s. Find (a) the average velocity, and (b) the average acceleration, between  $t = 3.00$  s and  $t = 20.0$  s.



1 Average velocity:-

$$\textcircled{1} \bar{v} = \frac{\Delta x}{\Delta t} = \frac{25 - 0}{3 - 0} = \frac{25}{3} = 8.3 \text{ m/s} \quad \textcircled{2} \frac{385 - 25}{20 - 3} = \frac{360}{17} = 21.2 \text{ m/s}$$

2 Average acceleration:- (3s  $\rightarrow$  20s)

$$\bar{a} = \frac{\Delta v}{\Delta t} = \frac{45 - 11}{20 - 3} = \frac{34}{17} = 2 \text{ m/s}^2$$



# Newton's Laws

\* Kinematic: Studying motion of objects regardless of the force causing the motion [need force]

\* Dynamics: Studying motion of objects taking into account the force causing the <sup>motion</sup> ~~motion~~

Force :- vector

Inertial frame  $\rightarrow$  doesn't accelerate  
when Newton's Laws are  
Valid.  $\rightarrow$  اعطاء أجوبة  $\checkmark$

\* there's no acceleration  
without force

\* to have an order you need a force

\* forces cause the motion  
\* if I'm standing I can't move  
until a force affect on me

Speed = magnitude

\* there's no force to move the object  
forward and this's why the object go back

because we need  
acceleration

no acceleration  $\Rightarrow$  no force      when there's there's  
acceleration = force

Newton's 1st Law :-

an object at last remain, so, an object moving at constant velocity

important

$\rightarrow$  (mag + dir) also remaining so, unless accelerated upon by net force

magnitude  
direction  $\uparrow$

\* the law of inertial  $\rightarrow$  قانون القصور الذاتي

[resistant of logice motion]

يعني الجسم قاصر عن تغير حالة الحركية الا بوجود قوة

Mass :- measure in the resistance of an object to change in motion  
distant to an object to motion

مقاومتها / مقاومتها للتغير

Scalar

Newton's 2nd Law :-

\* object's can't change there motion

لا يتسارع أو يتباطى الا اذا أثرت عليه قوة خارجية

multiplication  
علاقة الضرب

ex of 'x'  
vector by  
Scalar

$\vec{F} = m\vec{a}$       acceleration

we can also write  $\vec{a} = \frac{1}{m}\vec{F}$

\* Q: what's the direction of the acceleration? resultant force

Force  
gravitnated  
Force

الكتلة  
mass

وزن  
wieght

$(W = mg)$

Scalar  
\* constant  
regardless  
on position

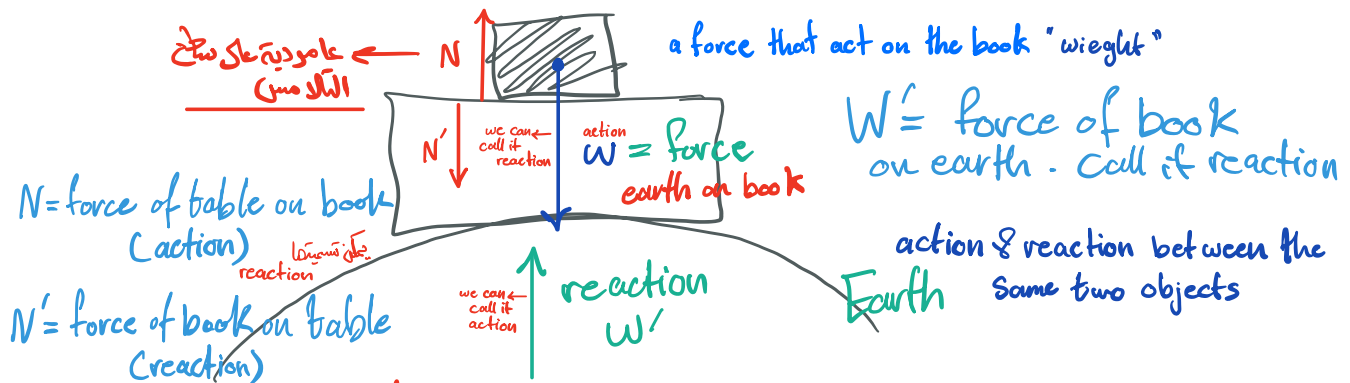
vector  
\* depends on position "Variable"  
(on earth  $\rightarrow$  on moon)  
يعتمد على تسارع الجاذبية

$F_x = m\vec{a}_x$   
 $F_y = m\vec{a}_y$   
 $F_z = m\vec{a}_z$

Newton = N  
1 Kg · m/s<sup>2</sup>  
 $\frac{M \cdot L}{T^2}$  it's compound  
dimension of newton

# Newton's 3rd Law

action - reaction = forces are equal and opposite



action - reaction NEVER act on the same object

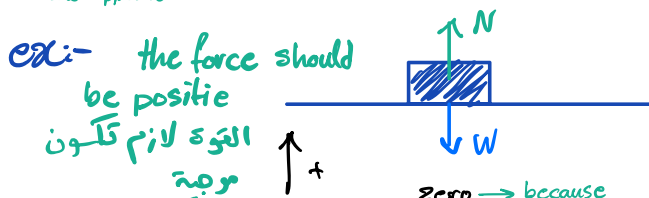
they have same mag & diff direction

مساوات في المقار ومعاكسات في الإجابة  
 $W \& W'$   
 $N \& N'$  } they are equal and opposite

Normal reaction/ Force :- normal to the surface of contact

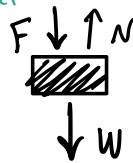
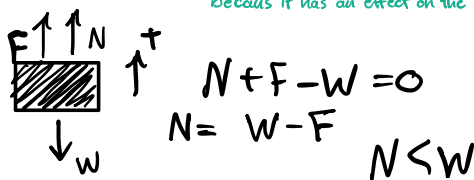
عامودية على سطح التماس

Contact Force  
 الكتاب يؤثر على الطاولة بقوة إلى الأسفل و الطاولة تؤثر على الكتاب بقوة إلى الأعلى قوة تماس



$N - W = ma = 0$   
 $N - W = 0 \Rightarrow N = W$   
 zero → because acceleration is negative

غير صحيح انه N و W عارة عن action-reaction because it has an effect on the same object



رسمه تظهر كل القوة على الجسم

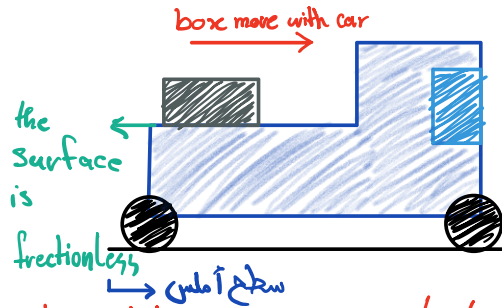
\* Free - body digraph

Show all existing force acting on object

the one that's using the Inertial fram doesn't move / accelerate

الشخص الذي بحسب لا يتحرك

this was in the beginning of the lecture:-



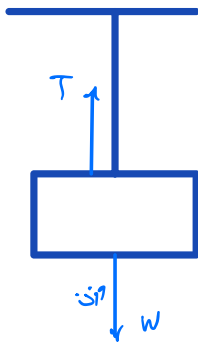
Car moves  
السيارة تاروقتها.  
الامتلاك أنزلت

if the car stops the box will go forward because there's nothing to stop it accelerate

سطح لا يجري على  
قوة إحتلاك

\* to have an acceleration of deceleration you need \*FORCE\*

# Examples



static equilibrium  
Find the tension in the string

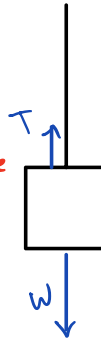
static equilibrium  
 $\Sigma F = 0$   
 $F_{net} = 0$

$\Sigma F = ma$   
 $F_{net} = ma$   
 $T - W = ma \rightarrow (0)$   
 $T = W \Rightarrow T = mg$

$W = mg$

Find T

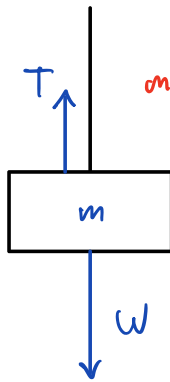
if system is moving  $\Rightarrow$  the direction of the motion to be positive



moving up at a constant velocity

Dynamic equilibrium  $\rightarrow$  اتزان

$T - W = 0$   
 $T = W$



$g = 9.8$   
moving up and accelerate  $\leftrightarrow$  if it was decelerating

at  $2 \text{ m/s}^2$  Find T

$T - mg = ma$

$T = mg + ma$

$40 + 4 \times 2 = 48 \text{ N}$

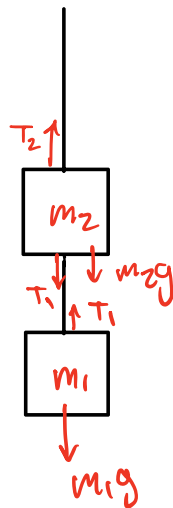
$T - mg = ma$

$T = mg + ma = 40 + 4(-2)$

$= 32$

$m_1 = 6 \text{ kg}$

$m_2 = 4 \text{ kg}$



static

$\uparrow$  for  $m_1$

$T_1 - m_1g = 0$

$T_1 = 6 \times 9.8 = 60 \text{ N}$

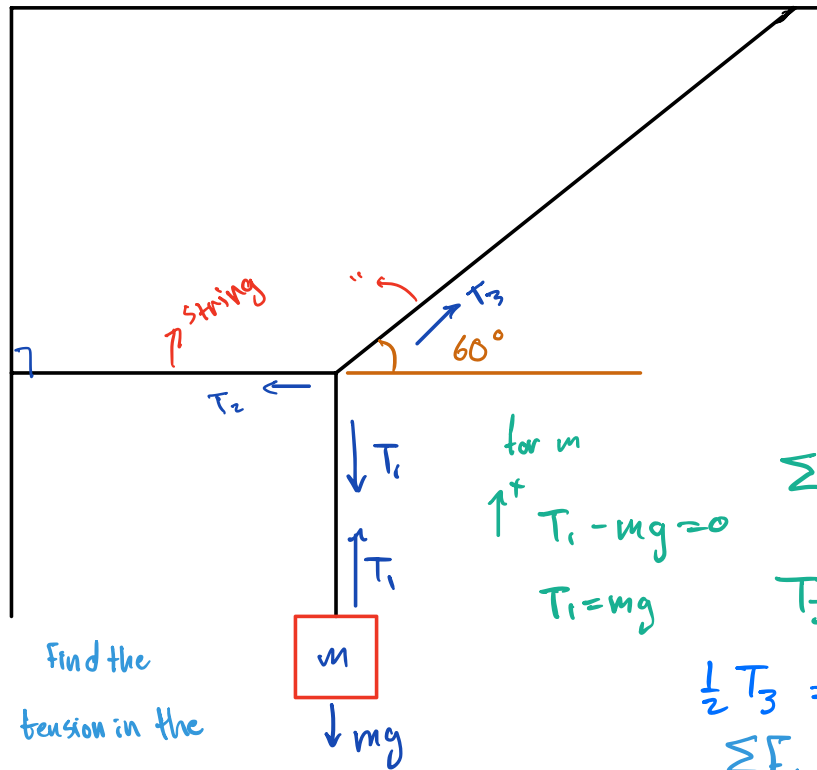
$\uparrow$  for  $m_2$

$T_2 - T_1 - m_2g = 0$

$T_2 = 60 + 40 = 100 \text{ N}$

$\textcircled{1} + \textcircled{2} \Rightarrow T_2 - m_1g - m_2g = 0$

$T_2 = (m_1 + m_2)g$



Find the tension in the strings

for m  
 $\uparrow T_1 - mg = 0$   
 $T_1 = mg$

$$\sum F_x = \text{max} = 0$$

$$T_3 \cos(60) - T_2 = 0$$

$$\frac{1}{2} T_3 = T_2 \Rightarrow T_3 = 2 T_2$$

$$\sum F_y = \text{max}_y$$

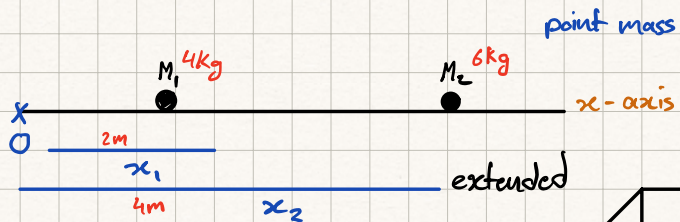
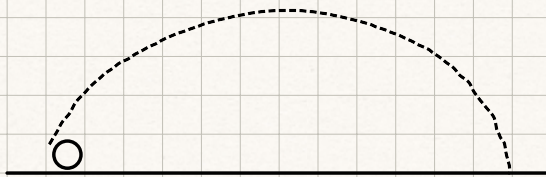
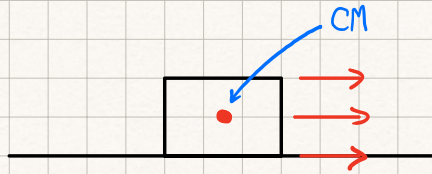
$$\uparrow T_3 \sin 60 - T_1 = 0$$

$$T_3 \times \frac{\sqrt{3}}{2} = T_1 = mg$$

$$T_3 = \frac{2}{\sqrt{3}} mg$$

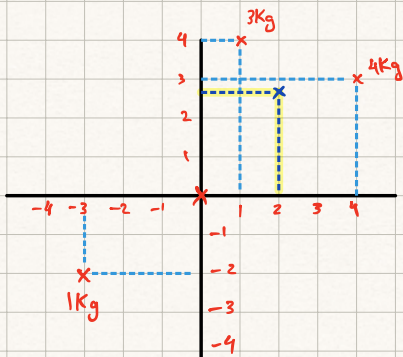
$$T_2 = \frac{1}{2} T_3 = \frac{1}{\sqrt{3}} mg$$

# Center of Mass



$$x_{CM} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2}$$

$$x_{CM} = \frac{4(2) + 6(4)}{10} = \frac{32}{10} = 3.2 \text{ m}$$



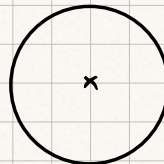
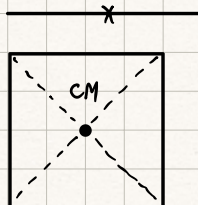
$$x_{CM} = \frac{3(1) + 4(4) + 1(-3)}{8} = 2 \text{ m}$$

$$y_{CM} = \frac{3(4) + 4(3) + 1(-2)}{8} = 2.75 \text{ m}$$

## Regular Object

Uniform

türk → şipir



### 3 Center of mass of legs

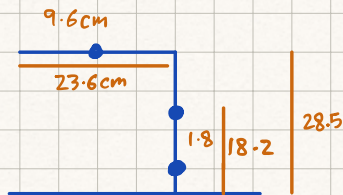
a) stretched



$$x_{CM} = \frac{M_{UL} x_{UL} + M_{LL} x_{LL} + M_F x_F}{M_{UL} + M_{LL} + M_F} = \frac{21.5(9.6) + 9.6(33.9) + 3.4(50.3)}{21.5 + 9.6 + 3.4} = 20.4 \text{ cm}$$

↳  $\times \frac{20.4}{100} \times 170$

b) bend



$$x_{CM} = 14.9 \text{ units}$$

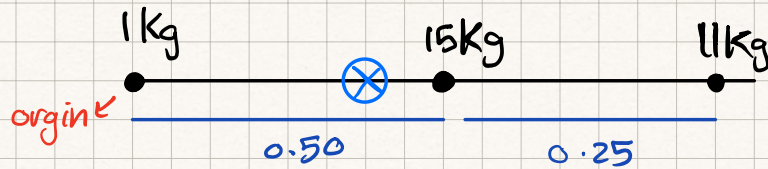
$$x_{CM} = \frac{14.9}{100} \times 1.7 \text{ m} = 0.25 \text{ m}$$

$$y_{CM} = 23 \text{ units}$$

$$y_{CM} = \frac{23}{100} \times 1.7 \text{ m} = 0.39 \text{ m}$$

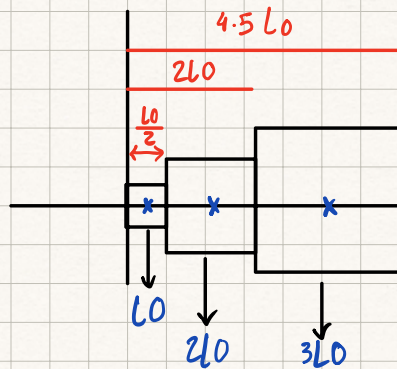
# Problems

46]



$$x_{CM} = \frac{1(0) + 1.5(0.50) + 1.1(0.75)}{1 + 1.5 + 1.1} = 0.438 \text{ m}$$

48]



$$m = \rho V \quad \text{density}$$

$$m_i = \rho l^3$$

$$m_2 = \rho (2L_0)^3 = 8 \rho L_0^3 = 8m_1$$

$$m_3 = \rho (3L_0)^3 = 27 \rho L_0^3 = 27m_1$$

$$x_{CM} = \frac{m_1(\frac{L_0}{2}) + 8m_1(2L_0) + 27m_1(4.5L_0)}{m_1 + 8m_1 + 27m_1}$$

$$x_{CM} \approx 3.8L_0$$



51]

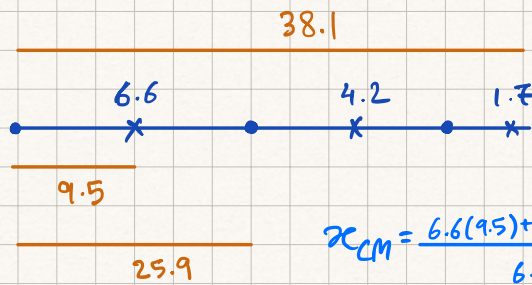
100g

$$M = m_{VL} + m_{LL} + m_F$$

$$= 21.5 + 9.6 + 3.4 = 34.5 \text{ Kg} \rightarrow 2 \text{ legs}$$

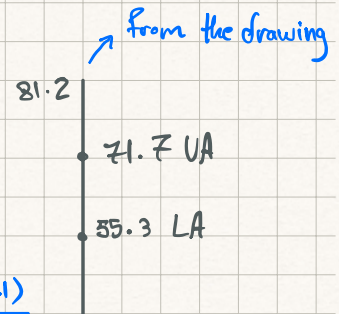
$$M_{\text{one leg}} = \frac{34.5}{2} = 17.25 \text{ Kg}$$

52]



$$x_{CM} = \frac{6.6(9.5) + 4.2(25.9) + 1.7(38.1)}{6.6 + 4.2 + 1.7}$$

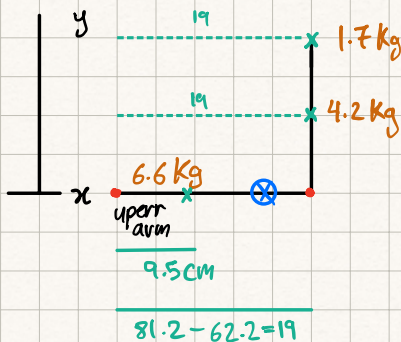
$$= 19 \text{ cm}$$



for 160 cm tall person :-

$$x_{CM} = \frac{19 \text{ cm}}{100} \times 160 = 30.4 \text{ cm}$$

53]



$$62.2 - 55.8 = 6.9 \text{ m}$$

$$\rightarrow 62.2 - 43.1 = 19.1 \text{ cm}$$

for 155 cm tall person

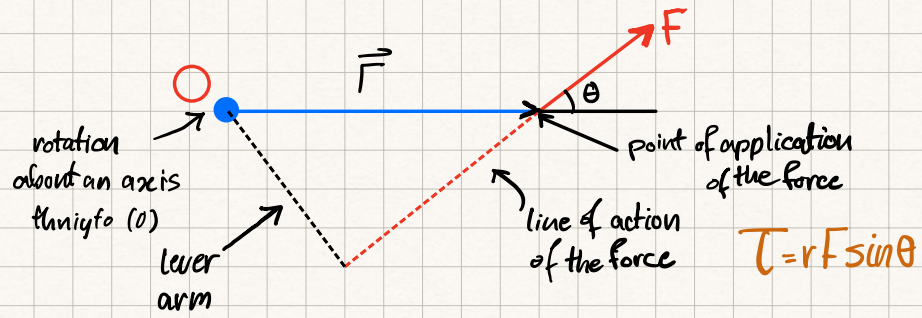
$$x_{CM} = \frac{14}{100} \times 155 = 21.7 \text{ cm}$$

$$y_{CM} = \frac{4.9}{100} \times 155 = 7.6 \text{ cm}$$

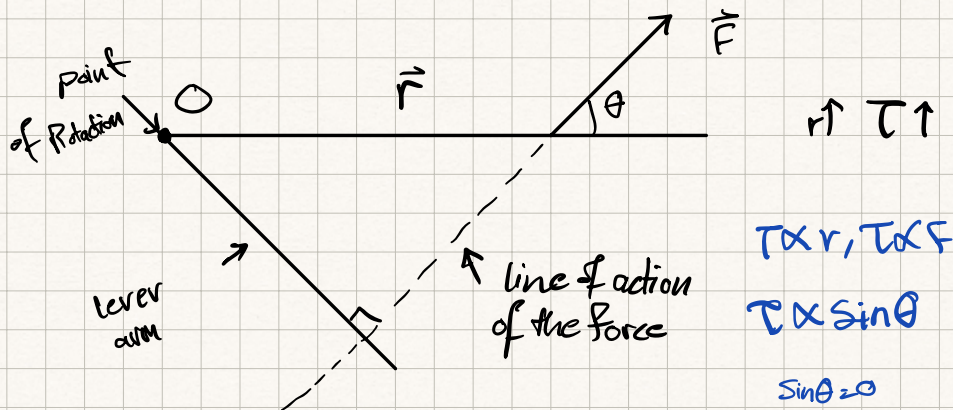
$$x_{CM} = \frac{6.6(9.5) + 4.2(19) + 1.7(19)}{6.6 + 4.2 + 1.7} = 14.0 \text{ m}$$

$$y_{CM} = \frac{6.6(0) + 4.2(6.9) + 1.7(19.1)}{6.6 + 4.2 + 1.7} = 4.9 \text{ cm}$$

Ch8 torque  
عزم الدوران

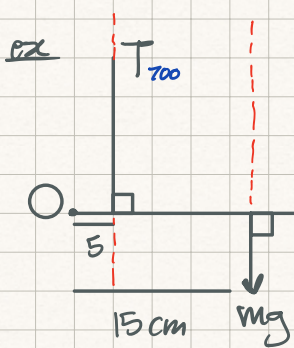


chZ-2



$\tau \propto r, \tau \propto F$   
 $\tau \propto \sin \theta$

$\sin \theta = 0$   
 $\theta = 0 \Rightarrow \tau = 0$   
 $\theta = 180^\circ \rightarrow \sin 180^\circ = 0$   
 $\tau = 0$



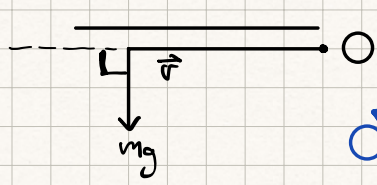
$\tau_{mg} = mg \times (0.15) \sin 90$   
 $= -0.15 mg$   
 $= -2.25 \text{ N}\cdot\text{m}$

$\tau_T = (700)(0.05) \sin 90$   
 $= 35 \text{ N}\cdot\text{m}$

$\tau_{\text{net}} = 35 - 2.25 = 32.75 \text{ N}\cdot\text{m}$

$\tau \rightarrow \text{vector}$

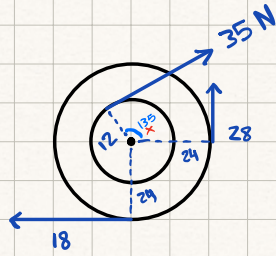
24]



$\tau_{\text{max}} = \theta = 90$

$\tau_{\text{max}} = mg(0.1F) \sin 90$   
 $= 86.6 \text{ N}\cdot\text{m}$

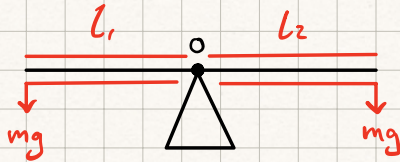
25]



$$\circlearrowleft \tau = (28)(0.24) \sin 90 - (35)(0.12) \sin 90 - (18)(0.24) \sin 90 = -1.8 \text{ N}\cdot\text{m}$$

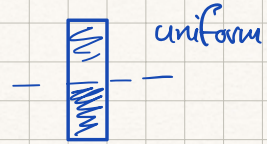
$$\tau_{\text{net}} = \tau + \tau_f = -1.8 + 0.6 = -1.2 \text{ N}\cdot\text{m}$$

27]



$$\circlearrowleft \tau_{\text{net}} = -mgl_2 + mgl_1$$

$$mgl_1 - mgl_2$$

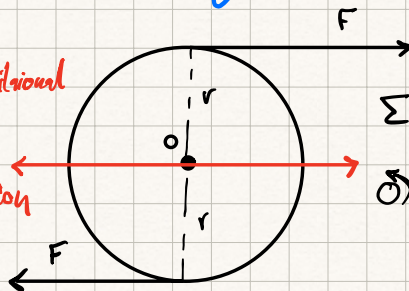


## Static Equilibrium

Static equilibrium

$$\sum \vec{F} = 0 \quad \times \text{translational}$$

$$\sum \tau = \tau_{\text{net}} = 0 \quad \times \text{rotation}$$



$$\sum F = 0 \quad \text{no translational motion}$$

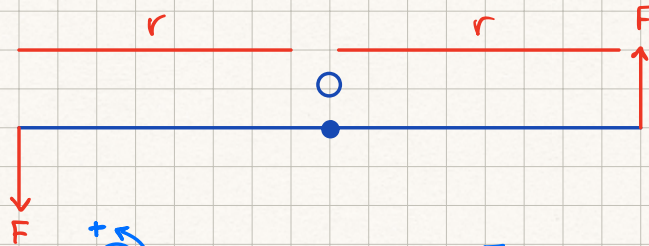
$$\circlearrowleft \tau = -rF \sin 90 - rF$$

$-2rF$   
 $\downarrow$   
 clockwise rotation

we have rotation motion  
 $\Rightarrow$   
 No static equilibrium

# Ch9

المساحة المرافقة



$$\tau = rF + rF = 2rF$$

$$\tau = DF$$

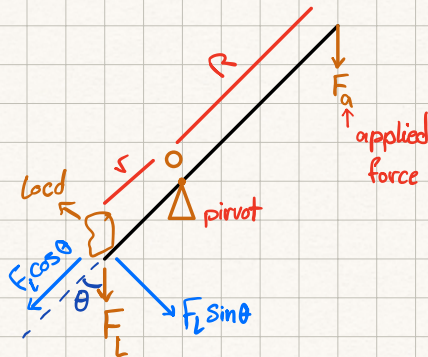
perpendicular distance  
between the two forces

this is called  
couple

$$\Sigma F = 0$$

$$\Sigma \tau \neq 0$$

## Lever



assume static equilibrium

$$\Sigma \tau = 0$$

$$Fr \sin \theta$$

$$r(F \sin \theta)$$

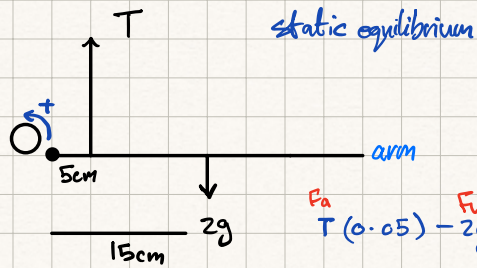
$$\tau = Fr \sin \theta - F_a R \sin \theta = 0$$

$$rF_L = RF_a$$

$$\frac{F_L}{F_a} = \frac{R}{r} \Rightarrow MA \text{ mechanical advantage}$$

$$MA > 1 \checkmark$$

ex



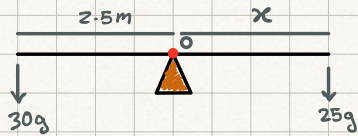
static equilibrium

$$T(0.05) - 2g(0.15) = 0$$

$$T = \frac{0.15}{0.05} = 3(2g)$$

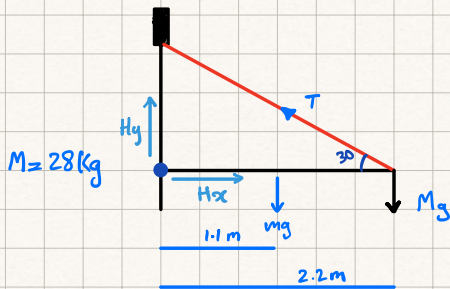
$$MA = \frac{F_L}{F_a} = \frac{2g}{3(2g)} = \frac{1}{3} < 1$$

ex



$$30g(2.5) - 25g x = 0 \quad \frac{30(2.5)}{25} = \frac{25x}{25} = 3m$$

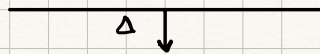
ex



$$\Sigma F_x = 0$$

$$\Sigma T = 0$$

Hinge force / joint force



$$0^+ (T \sin 30)(2.2) - M_g(2.2) - mg(1.1) = 0$$

$$T = 794 \text{ N}$$

$$\Sigma F_x = 0$$

$$H_x - T \cos 30 = 0$$

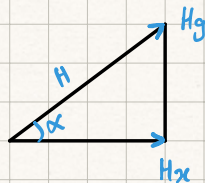
$$H_x (794) \frac{\sqrt{3}}{2} \sim 687.6 \text{ N}$$

+↑

$$\Sigma F_y = 0$$

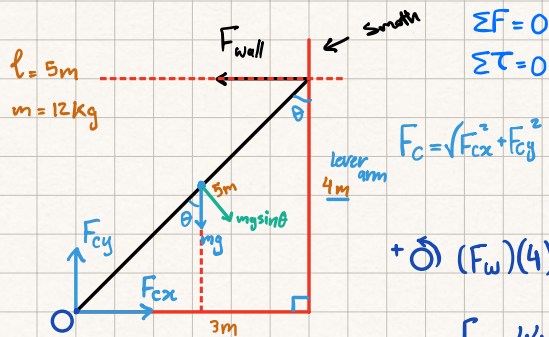
$$H_y + T \sin 30 - mg - M_g = 0$$

$$H_y = 122.4 \text{ N}$$



$$H = \sqrt{H_x^2 + H_y^2}$$

$$\tan \alpha = \frac{H_y}{H_x} \quad \alpha \sim 10.1$$



$$\Sigma F = 0$$

$$\Sigma \tau = 0$$

$$F_c = \sqrt{F_{cx}^2 + F_{cy}^2}$$

$$+\odot (F_w)(4) - (mg \sin \theta) \left(\frac{5}{2}\right) = 0$$

$$F_w = 44.1 \text{ N}$$

$$\Sigma F_x = 0$$

$$+\rightarrow F_{cx} - F_w = 0$$

$$F_{cx} = F_w = 44.1$$

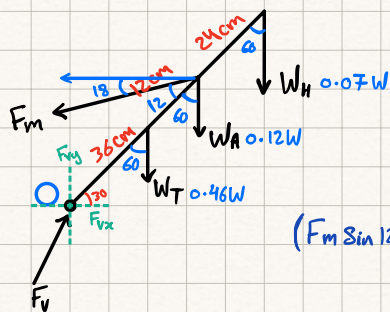
$$\Sigma F_y = 0$$

$$F_{cy} - mg = 0$$

$$F_{cy} = mg = 12g$$

$$F_c = 125.6 \text{ N}$$

$$\tan \alpha = \left| \frac{F_{cy}}{F_{cx}} \right| = 2.84$$



Static equilibrium

$$\Sigma \tau = 0$$

$$\Sigma F = 0$$

$$(F_m \sin 12)(0.48) - (W_T \sin 60)(0.36) - (W_A \sin 60)(0.48) - (W_H \sin 60)(0.72) = 0$$

$$F_m = 2.37 w$$

$$\Sigma F_x = 0$$

$$+\rightarrow F_{vx} - F_m \cos 18 = 0$$

$$F_{vx} = 2.25 w$$

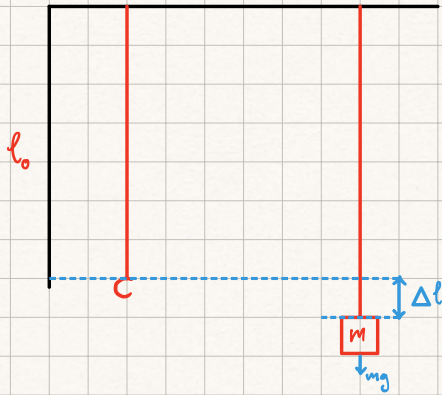
$$F_v = \sqrt{F_{vx}^2 + F_{vy}^2} \sim 2.7 w$$

$$+\uparrow F_{vy} - W_T - W_A - W_H - F_m \sin 18 = 0$$

$$F_{vy} = 1.38 w$$

# Elasticity

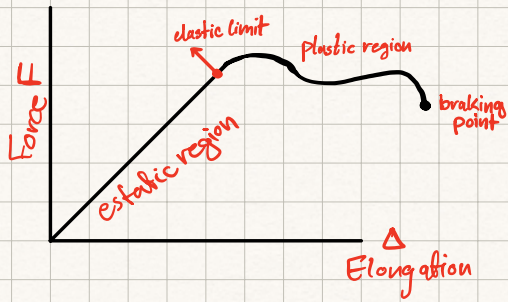
Stress, Strain



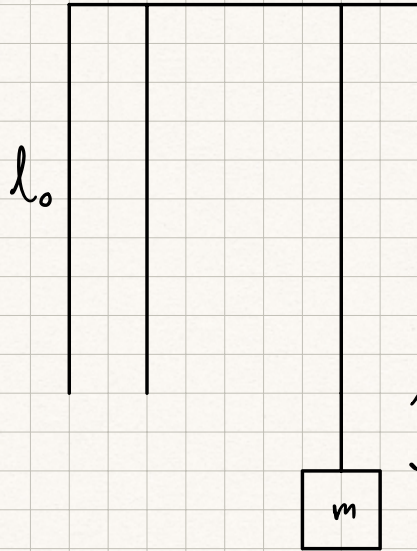
Hook's Law  
 $F = k \Delta l$   
↙  
magnitude

Hook's Law  
 $F = -kx$

$\Delta l \ll l_0$







$$\Delta l \propto \frac{l_0 F}{A}$$

$$\Delta l = \frac{1}{E} l_0 \left( \frac{F}{A} \right) \frac{N}{m^2}$$

↑ young's modulus     ↓ stress

$$\frac{\Delta l}{l_0} = \text{strain}$$

$$E = \frac{F}{A} \cdot \frac{l_0}{\Delta l} = \frac{F/A}{\left( \frac{\Delta l}{l_0} \right)} = \frac{\text{stress}}{\text{strain}}$$

Modulus  $E (N/m^2)$

- Steel  $200 \times 10^9$

- bone (limb)  $15 \times 10^9$

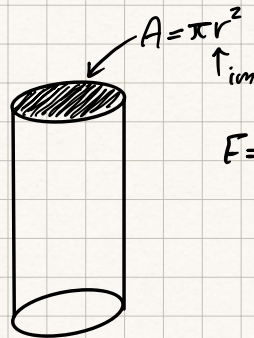
كلما كانت المادة أقوى

example :-

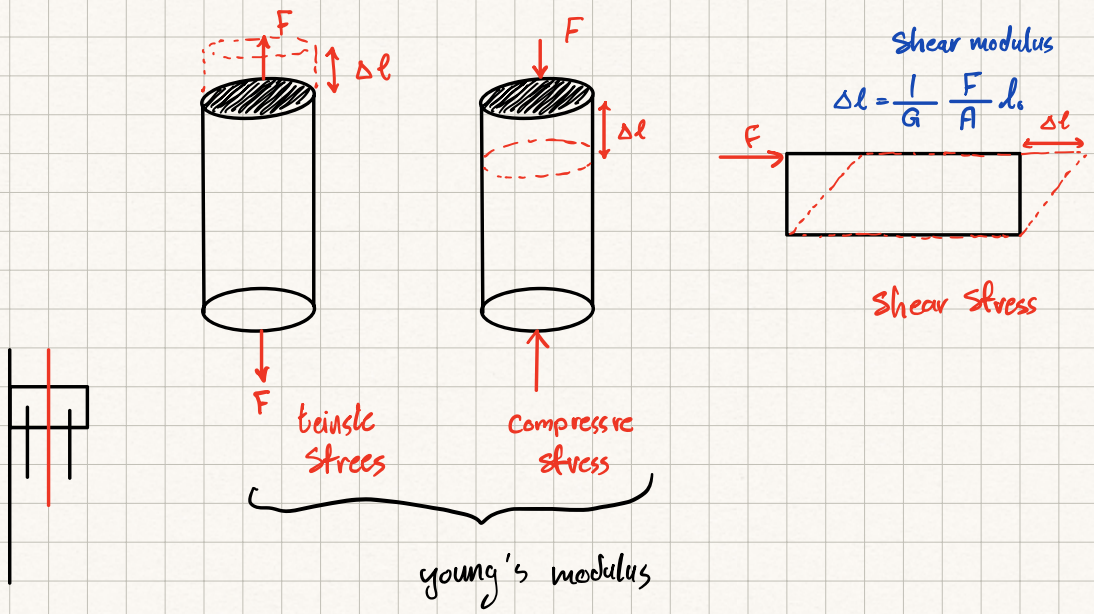
$$l_0 = 1.6 \text{ m}$$

$$D = 0.2 \text{ cm} \Rightarrow r = 0.1 \text{ cm}$$

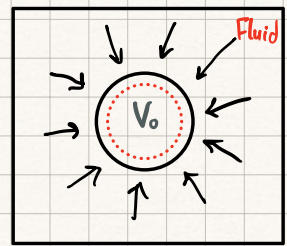
$$\Delta l = 0.25 \text{ cm}$$



$$F = 980 \text{ N}$$



# Bulk



$P = \frac{F}{A}$  same as stress pressure

Original Volume  $V_0$

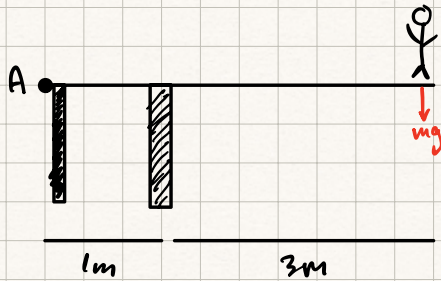
Change in Volume  $\Delta V$

$\frac{\Delta V}{V_0} = -\frac{1}{B} \Delta P$   
 bulk modulus

# Fracture

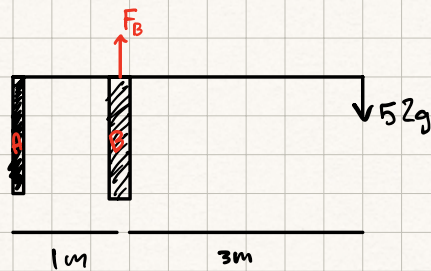
	tensile stress (N/m <sup>2</sup> )	Compressive stress	shear stress
Steel	$500 - 250 \times 10^6$	$500 \times 10^6$	$250 \times 10^6$
Bone	$130 \times 10^6$	$170 \times 10^6$	

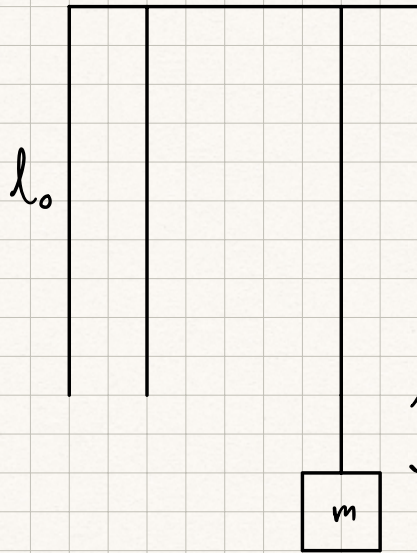
4)



$$\overset{+}{A} \quad -1800 = -(mg)(4)$$

$$m = \frac{1800}{4} \sim 45.9 \text{ kg}$$





$$\Delta l \propto \frac{l_0 F}{A}$$

$$\Delta l = \frac{1}{E} l_0 \left( \frac{F}{A} \right) \frac{N}{m^2}$$

↑  
young's  
modulus

↓  
stress

$$\frac{\Delta l}{l_0} = \text{strain}$$

$$E = \frac{F}{A} \cdot \frac{l_0}{\Delta l} = \frac{F/A}{\left( \frac{\Delta l}{l_0} \right)} = \frac{\text{stress}}{\text{strain}}$$

Modulus  $E (N/m^2)$

- Steel  $200 \times 10^9$

- bone (limb)  $15 \times 10^9$

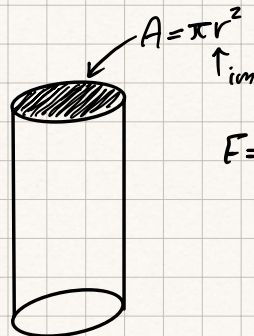
كلما كانت المادة أقوى

example :-

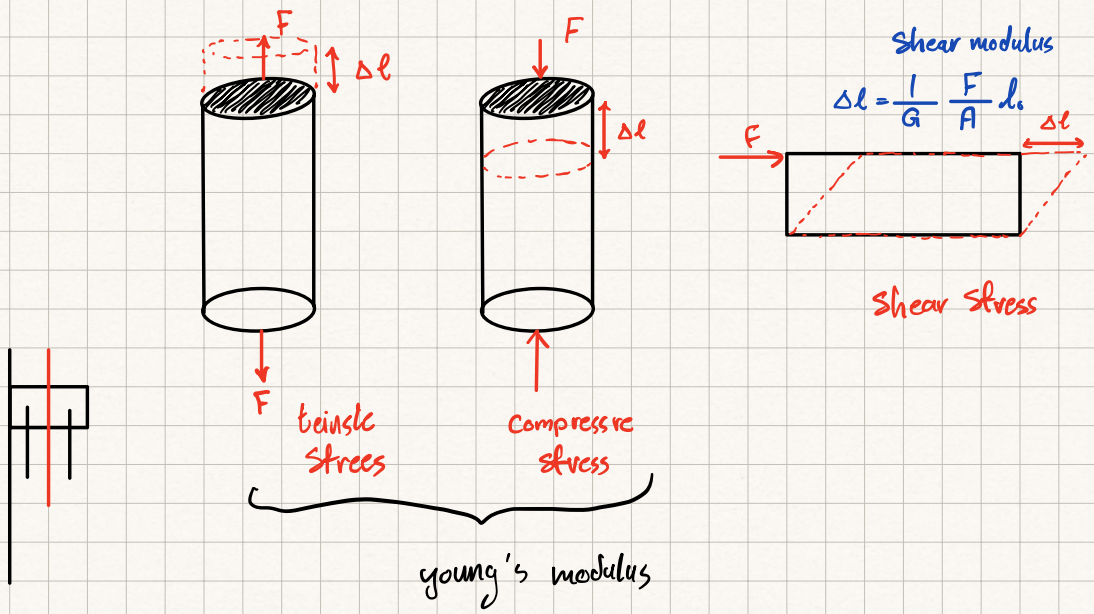
$$l_0 = 1.6 \text{ m}$$

$$D = 0.2 \text{ cm} \Rightarrow r = 0.1 \text{ cm}$$

$$\Delta l = 0.25 \text{ cm}$$



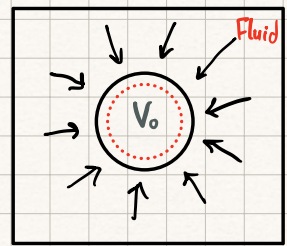
$$F = 980 \text{ N}$$



Shear modulus  

$$\Delta l = \frac{1}{G} \frac{F}{A} l_0$$

Bulk



$$P = \frac{F}{A}$$
 same as stress pressure

Original Volume  $V_0$

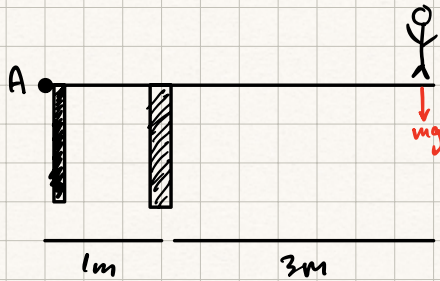
Change in Volume  $\Delta V$

$$\frac{\Delta V}{V_0} = - \frac{1}{B} \Delta P$$
  
 bulk modulus

# Fracture

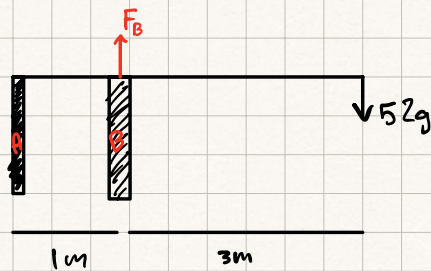
	tensile stress (N/m <sup>2</sup> )	Compressive stress	shear stress
Steel	500-250 × 10 <sup>6</sup>	500 × 10 <sup>6</sup>	250 × 10 <sup>6</sup>
Bone	130 × 10 <sup>6</sup>	170 × 10 <sup>6</sup>	

4)



$$\overset{+}{A}) -1800 = -(mg)(4)$$

$$m = \frac{1800}{4} \sim 45.9 \text{ kg}$$



$$46] \quad \text{stress} = \frac{F}{A} \quad F_{\text{max}} = A \times \text{stress} \rightarrow \text{maximum stress}$$

$$F_{\text{max}} = A \times 170 \times 10^6$$

$$50] \quad 3300 \frac{\text{N}}{\text{m}^2} \quad \text{stress} \frac{F}{A}$$

$$\frac{3300}{7} =$$

# Fluids سوائل

states of matter

Gas, no fixed volume nor shape

liquid, fixed volume, no fixed shape

solid, fixed volume & shape

plasma

density  $\frac{\text{mass}}{\text{volume}}$

$$\rho = \frac{m}{V} \text{ Kg/m}^3$$

Specific gravity

$$SG = \frac{\text{density of material}}{\text{density of water at } 4^\circ\text{C}}$$

ex:-

Iron

$$SG = \frac{7800}{1000} = 7.8$$

Pressure

$$\frac{\text{Force}}{\text{area}} = \frac{N}{m^2} = \text{Pascal}$$

ex:-

$$m = 60 \text{ kg}$$

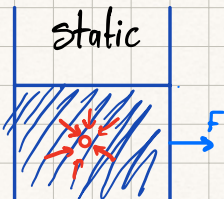
$$A = 500 \text{ cm}^2$$

two features

Static fluids

$$\sum F = 0$$

$$P = 0$$



① at any one point at static the pressure in all direction

② the force of any liquid is (منه القوة في كل الاتجاهات)

a) both feet

$$\frac{F}{A} = \frac{mg}{A} = \frac{60 \times 9.8}{500 \times 10^{-4}}$$

$$= 12000 \text{ N/m}^2 \sim \text{Pa}$$

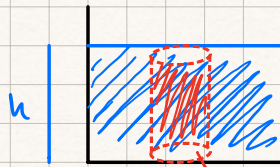
b) one foot

$$P_1 = \frac{mg}{\frac{A}{2}} = 2 \frac{mg}{A}$$

$$= 24000 \text{ Pa}$$

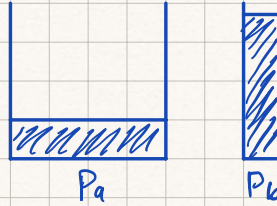


# pressure due (a static) fluids



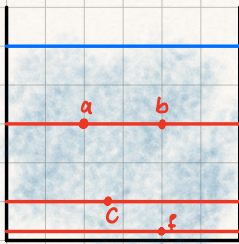
→ Area  
find the pressure on the base due to the fluid

$$P = \frac{F}{A} = \frac{mg}{A} = \frac{\rho Vg}{A} = \frac{\rho(Ah)g}{A} = \rho gh$$

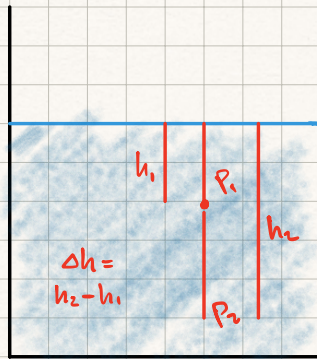


كثافة الزجاج 1.29  
كثافة الزيت 0.9  
كثافة الماء 1

$P_b > P_a$  as pressure



$$P_a = P_b < P_c < P_d$$



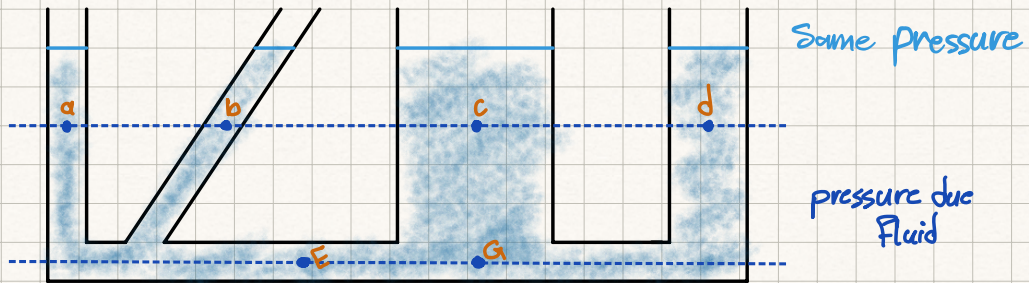
$$P_1 = \rho_F g h_1$$

$$P_2 = \rho_F g h_2$$

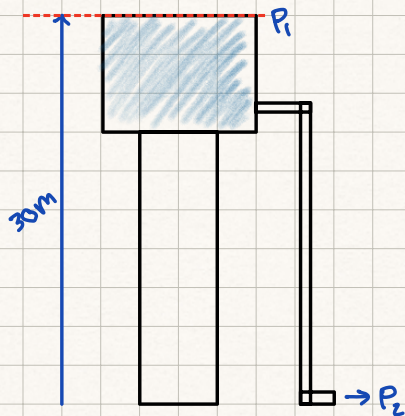
$$P_2 - P_1 = \rho_F g (h_2 - h_1)$$

$$P_2 - P_1 = \rho_F g \Delta h$$

$$P_2 = P_1 + \rho_F g \Delta h$$



$$P_E = P_G$$



$$P_2 - P_1 = \rho_F g \Delta h$$

$$= (1000)(9.8)(30)$$

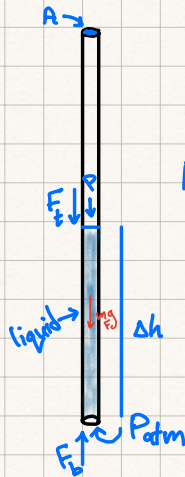
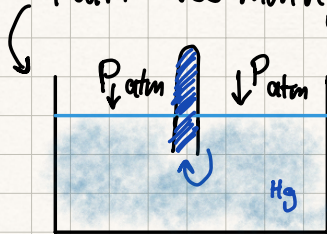
$$= 2.9 \times 10^5 \text{ Pa}$$

# Atmosphere Pressure

$$1 \text{ atm} = 1.013 \times 10^5 \text{ Pa} = 1.013 \text{ bar}$$

$$1 \text{ bar} = 1 \times 10^5 \text{ Pa}$$

$$1 \text{ atm} = 760 \text{ mm Hg}$$



depends on pressure in side

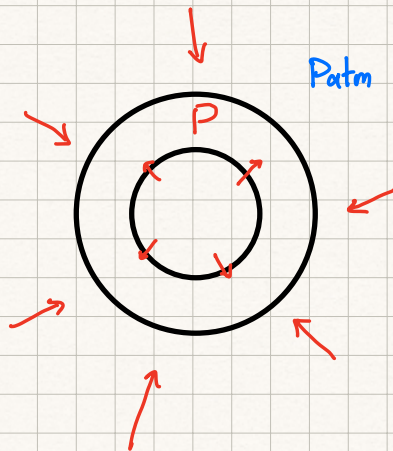
$$P_{\text{atm}} = P + \rho g \Delta h$$

$$P_{\text{atm}} A = P A + \rho g \Delta h A$$

$$F_b = F_t + \rho g V$$

$$F_b = F_t + m_F g$$

# Gauge Pressure

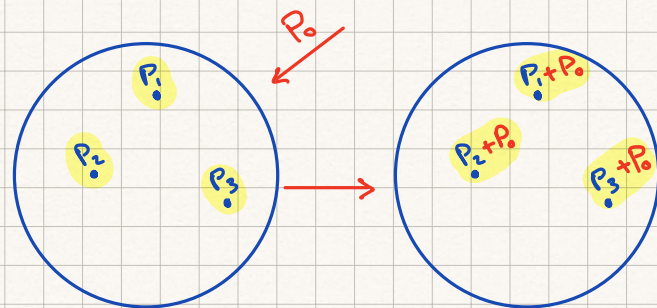


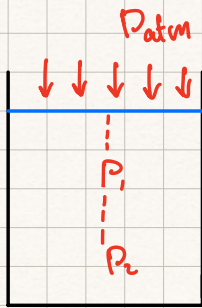
absolute pressure

$$P_{\text{gauge}} = P - P_{\text{atm}}$$

# Pascals' Principle

trapped fluid





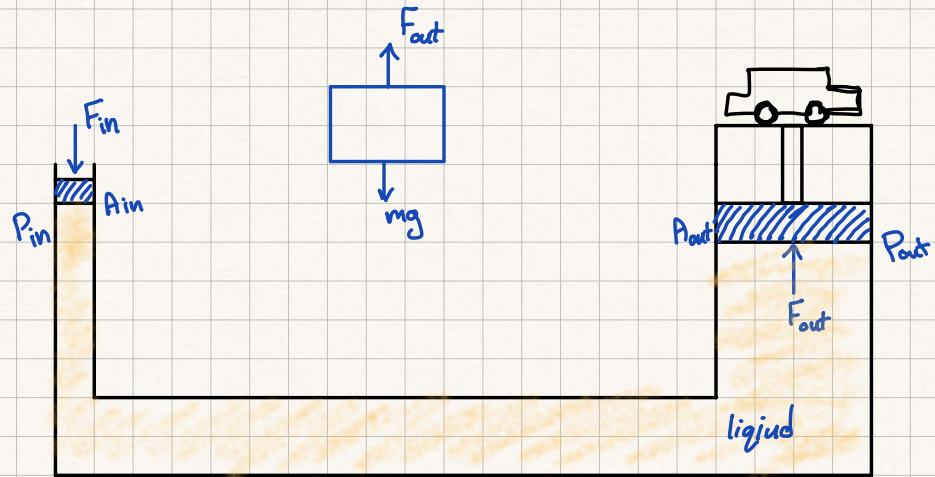
$$\left. \begin{aligned} P_1 &= \rho_f g h_1 \\ P_2 &= \rho_f g h_2 \end{aligned} \right\} \rightarrow \text{due to fluid}$$

$$P_{1 \text{ tot}} = P_1 + P_{\text{atm}}$$

$$P_{2 \text{ tot}} = P_2 + P_{\text{atm}}$$

$$P_{2 \text{ tot}} - P_{1 \text{ tot}} = (P_2 + P_{\text{atm}}) - (P_1 + P_{\text{atm}})$$

$$P_{2 \text{ tot}} - P_{1 \text{ tot}} = P_2 - P_1 = \rho_f g \Delta h$$



$$P_{in} = P_{out}$$

$$\frac{F_{in}}{A_{in}} = \frac{F_{out}}{A_{out}}$$

$$F_{out} = \frac{A_{out}}{A_{in}} F_{in}$$

$F_{out}$  lift the car upwards

$$W = 10,000 \text{ N}$$

$$A_{out} = 20 A_{in}$$

$$F_{in} = \frac{A_{in}}{A_{out}} F_{out}$$

$$= \frac{1}{20} (10,000)$$

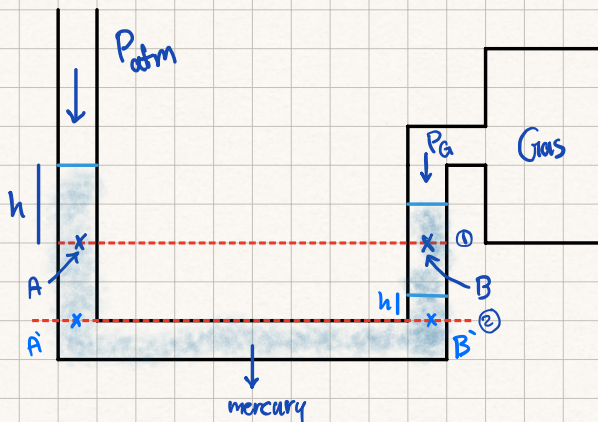
$$= 500 \text{ N}$$

$$MA = \frac{F_L}{F_A} =$$

$$\frac{10000}{500} = 20$$

$$A_{out} > A_{in} \Rightarrow F_{out} > F_{in}$$

## Open-tube manometer



$$P_A = P_B$$

$$P_{atm} + \rho_F g h = P_G$$

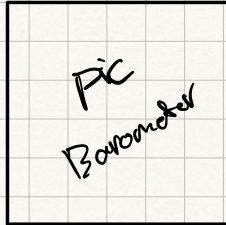
$$P_{atm} + \rho_F g h = P_G$$

$$P_A = P_B$$

$$P_{atm} = P_G + \rho_F g h$$

$$P_{atm} > P_G$$

# Barometer



$$P_A = P_B$$

$$\rho_F g h = P_{atm}$$

for mercury  $h = 760 \text{ mmHg}$   
 $1 \text{ atm} = 760 \text{ mmHg} = 1.013 \times 10^5 \text{ Pa} = 1.013 \text{ bar}$

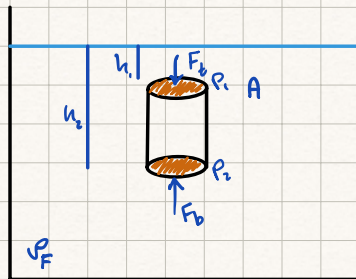
for water find h

$$\rho_w g h_w = 1.013 \times 10^5$$

1000 9.8 ?

$$h \sim 10.3 \text{ m}$$

## Buoyancy and Archimede's principle



$$P_t = \rho_F g h_1$$

$$F_t = P_t A = \rho_F g h_1 A$$

$$P_b = \rho_F g h_2$$

$$F_b = \rho_F g h_2 A$$

$$P_b > P_t \Rightarrow F_b > F_t$$

there's always resultant force upwards

resultant force due liquid

$$F_B = F_b - F_t = \rho_F g A (h_2 - h_1)$$

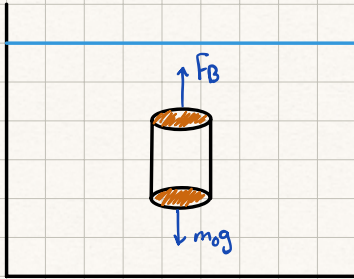
buoyant force

$$F_B = \rho_F g A h$$

$$F_B = \rho_F g V = \rho_F V g = m_F g$$

mass of displaced fluid

$F_B = \text{weigh of displaced fluid}$

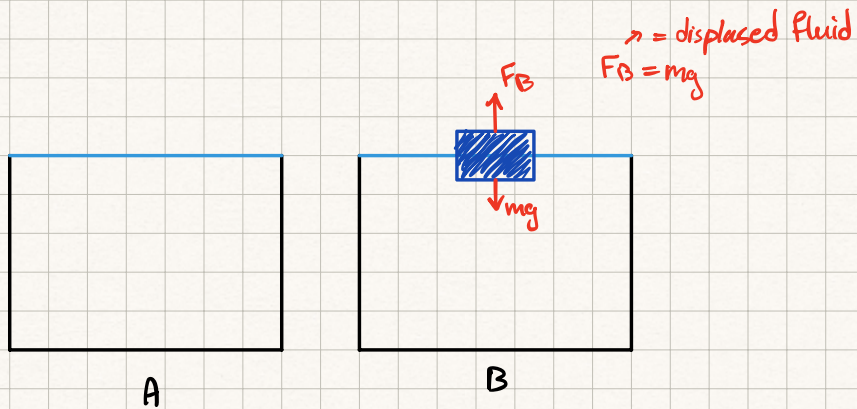


$$+\uparrow F_R = F_B - m_0g = \rho_F V g - \rho_0 V g$$

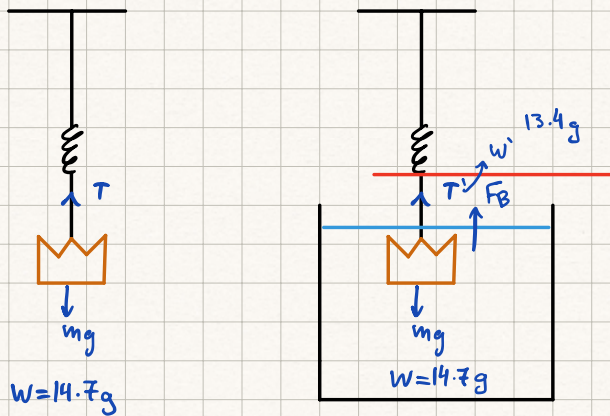
$$F_R = (\rho_F - \rho_0) V g$$

$$\rho_F > \rho_0 \Rightarrow F_R > 0 \quad \uparrow \text{object floats}$$

$$\rho_F < \rho_0 \Rightarrow F_R < 0 \quad \downarrow \text{object sinks}$$



ex



$$W = T = mg = \rho_0 V g \quad W = \rho_0 V g \quad \textcircled{1}$$

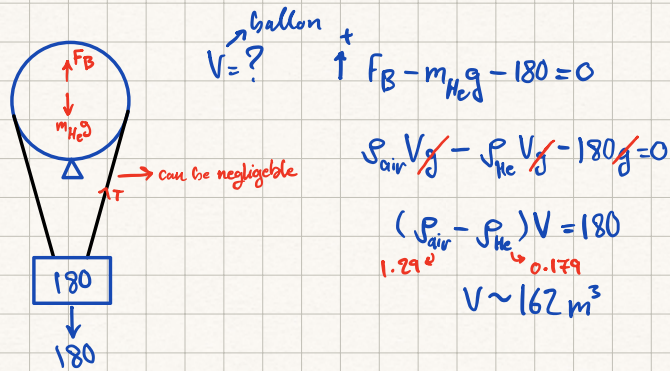
$$W = W' + F_B \quad W - W' = F_B = \rho_f V g \quad W - W' = \rho_f V g \quad \textcircled{2}$$

$$\frac{W}{W - W'} = \frac{\rho_0}{\rho_f} = \frac{14.7g}{14.7g - 13.4g} \Rightarrow \rho_0 = 11300 \text{ kg/m}^3$$

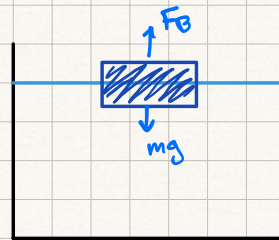
$F_B = \rho_f V g$  قوتی که از آب می‌آید



ex



## partial Submersion



$V_s =$  submerged Volume  
+ static equilibrium  
 $F_B = mg$

$$\rho_F V_s g = \rho_o V g$$

$$\frac{\rho_o}{\rho_F} = \frac{V_s}{V}$$

$V =$  volume of the object

$$\rho_{ice} \sim 0.9 \rho_{water}$$

$$\frac{\rho_{ice}}{\rho_{water}} = \frac{V_s}{V} \sim 0.9$$

Q of the He gets voice

# Fluids in motion

① Laminar Flow  
(Streamline)  $\cong$

parts don't cross

two assumptions

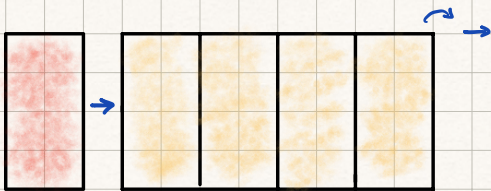
① Laminar flow

② non compressible fluid

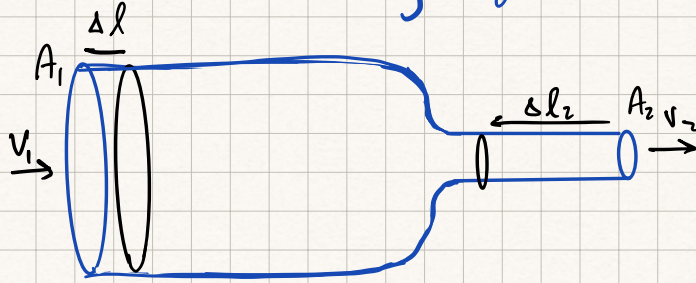
incompressible

(no change in Volume under pressure)

③ Nonviscous fluid



# Continuity Equation



Incompressible fluid

$$\frac{\Delta V_1}{\Delta t} = \frac{\Delta V_2}{\Delta t} \quad \text{Volume flow rate}$$

$$\rho_1 \frac{\Delta V_1}{\Delta t} = \frac{\Delta m_1}{\Delta t} \quad \text{mass flow rate}$$

$$\rho_1 \frac{\Delta V_1}{\Delta t} = \rho_2 \frac{\Delta V_2}{\Delta t}$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

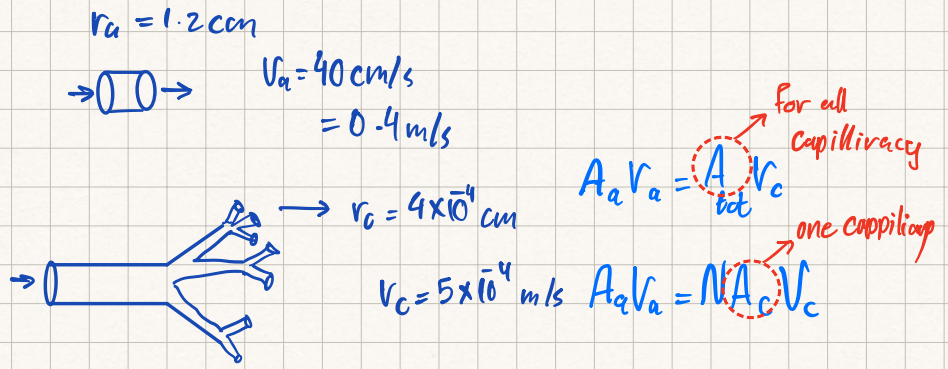
$$\rho_1 A_1 \frac{\Delta l_1}{\Delta t} = \rho_2 A_2 \frac{\Delta l_2}{\Delta t}$$

Incompressible fluid  $\Rightarrow \rho_1 = \rho_2 = \rho$

$$\boxed{A_1 v_1 = A_2 v_2} \quad \begin{array}{l} \text{المساحة} \\ \text{السرعة} \end{array} \quad \frac{\text{m}^3}{\text{s}}$$

ex

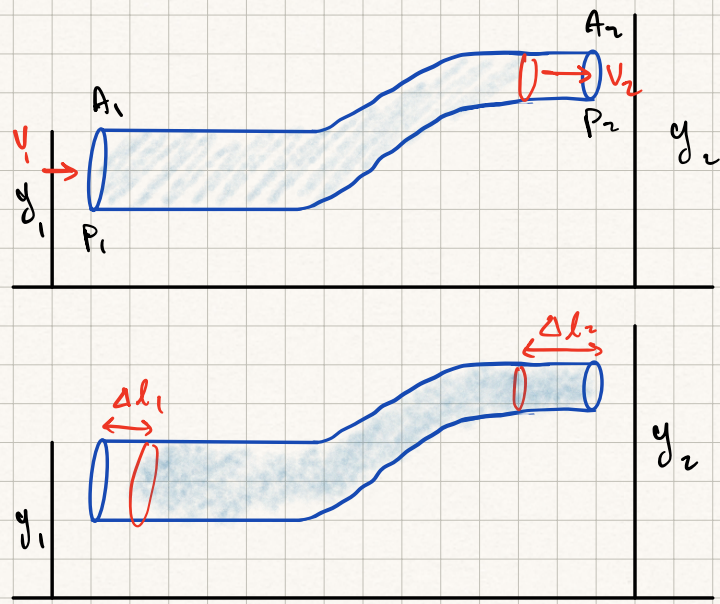
heart  $\Rightarrow$  aorta  $\Rightarrow$  arterioles  $\Rightarrow$  Capillaries



$$N = \frac{A_a v_a}{A_c v_c} = \frac{\pi r_a^2 v_a}{\pi r_c^2 v_c}$$

$$N \sim 7 \times 10^9$$

### Bernoulli's Equation



$$W_{total} = \Delta K = \frac{1}{2} m \Delta v^2$$

$$P_1 A_1 \Delta l_1 - P_2 A_2 \Delta l_2 - (m y_2 g - m y_1 g) = \frac{1}{2} m v_2^2 - \frac{1}{2} m v_1^2$$

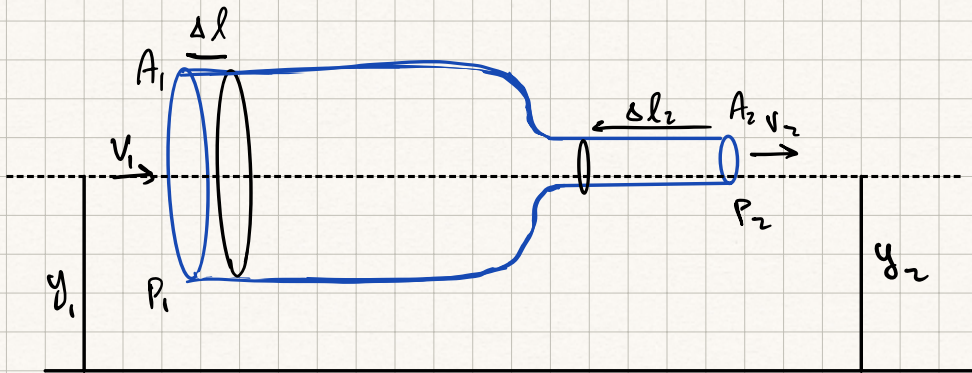
$$P_1 V - P_2 V + mgy_1 - mgy_2 = \frac{1}{2} mV_2^2 - \frac{1}{2} mV_1^2$$

$$\frac{N}{m^3} \cdot m \rightarrow P_1 V + mgy_1 + \frac{1}{2} mV_1^2 = P_2 V + mgy_2 + \frac{1}{2} mV_2^2 = \text{Constant}$$

N·m    J        J        J

$$\div V \Rightarrow \boxed{P_1 + \rho g y_1 + \frac{1}{2} \rho V_1^2 = P_2 + \rho g y_2 + \frac{1}{2} \rho V_2^2} \rightarrow \text{final form}$$

\* Incompressible & non viscous

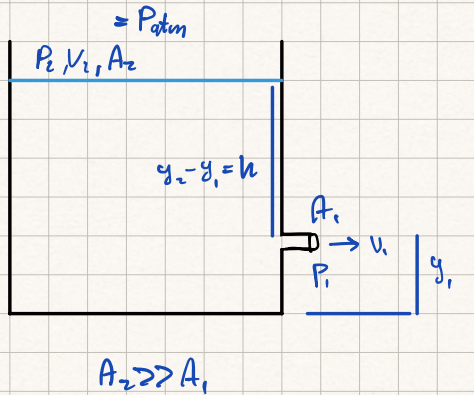


$$P_1 + \rho g y_1 + \frac{1}{2} \rho V_1^2 = P_2 + \rho g y_2 + \frac{1}{2} \rho V_2^2$$

$$P_1 + \frac{1}{2} \rho V_1^2 = P_2 + \frac{1}{2} \rho V_2^2$$

$$V_2 > V_1 \Rightarrow P_1 > P_2$$

# Torricelli principle



$$P_1 + \rho g y_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g y_2 + \frac{1}{2} \rho v_2^2$$

$$A_1 v_1 = A_2 v_2$$

$$v_2 = \frac{A_1}{A_2} v_1 \approx 0$$

~~$$P_{atm} + \rho g y_1 + \frac{1}{2} \rho v_1^2 = P_{atm} + \rho g y_2 + 0$$~~

~~$$\frac{1}{2} \rho v_1^2 = \rho g (y_2 - y_1)$$~~

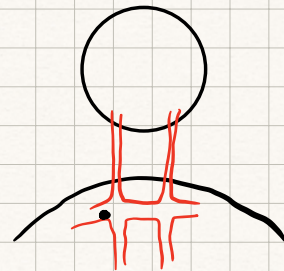
$$v_1^2 = 2g (y_2 - y_1)$$

$$v_1 = \sqrt{2gh}$$

TIA

Transient  
Ischemic  
attack

$v \uparrow$   $P \downarrow$   
 $v \downarrow$   $P \uparrow$



Poiseuille's eqn

- viscosity  $\uparrow$

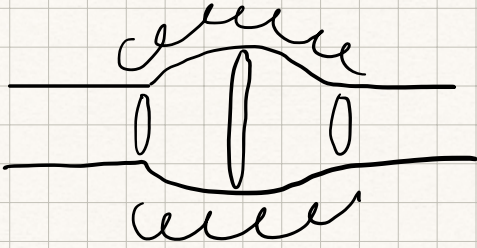
Volume flow rate  $\downarrow$



$$Q = \frac{\pi R^4 (P_1 - P_2)}{8 \eta l}$$

$$R \rightarrow \frac{R}{2}$$

$$Q \rightarrow \frac{Q}{16}$$



Q5)

	36g		36g		36g
			$M_w$ $= 98.44 - 35$ $= 63.44$		$M_F = 89.22 - 35$ $= 54.22g$


$$SG = \frac{\rho_F}{\rho_w} = \frac{M_F/V}{M_w/V} = 0.855$$

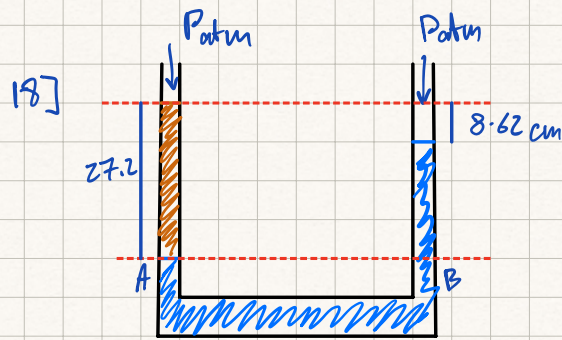
107

$P_{HO}$ $\downarrow$ $P_F$		1.75m	=	$P_F = P_H + \rho_{blood} g h$ $= 18170 Pa \times \frac{1.75}{1.013 \times 10^5}$
-----------------------------------	--	-------	---	--

$$= 136.3 \text{ mmHg}$$

ii)

$P_{atm}$ $\downarrow$  $\uparrow$	=	$F_{top} = P_{atm} \cdot A$ $F_{bottom} = P_{atm} \cdot A$
		$P_{atm} F_{top} = 1.013 \times 10^5 \text{ N/m}^2 \cdot (1.7 \times 2.6 \text{ m}^2)$ $= 44776 \text{ N}$

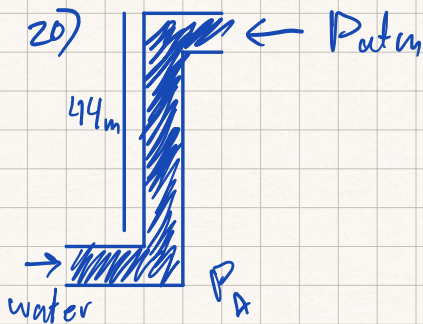


$$P_A = P_B$$

$$P_{atm} + \rho_{oil} g (27.2 \times 10^{-2}) =$$

$$P_{atm} + \rho_{water} g (27.2 - 8.62 \times 10^{-2})$$

$$\rho_{oil} = 683 \text{ kg/m}^3$$



$$P_{abs} = P_{atm} - P_{gage}$$

$$P_A = P_{atm} + \rho_{water} g h$$

$$P_A - P_{atm} = \rho_w g h$$

$$= 431200 \text{ Pa}$$

27)

