

$$H_0: \mu = \mu_0 \text{ vs. } H_1: \mu < \mu_0$$

$$\text{test statistic} = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$$

$$\text{critical value } 1-\alpha, 1-\frac{\alpha}{2}$$

$$df = n-1$$

$$H_0: p = p_0 \text{ vs. } H_1: p \neq p_0$$

$$\begin{aligned} \text{test statistic} &= \frac{\hat{p} - p}{\sqrt{\frac{\hat{p}\hat{q}}{n}}} \\ (z) &= \frac{|\hat{p} - p| - \frac{1}{2n}}{\sqrt{\frac{pq}{n}}} \end{aligned}$$

$$\text{critical value} = 1 - \frac{\alpha}{2}$$

$$H_0: \alpha_i = 0 \text{ vs. } H_1: \alpha_i \neq 0$$

$$\text{test statistic} = \frac{\text{Between MS}}{\text{Within MS}}$$

$$\text{critical value} = k-1, n-k, 1-\alpha$$

$$df = k-1, n-k$$

$$\text{Comparison: } t = \frac{\bar{y}_1 - \bar{y}_2}{\sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

$$\text{critical: } n-k, 1-\frac{\alpha}{2} \quad df = n-k$$

$$H_0: \mu_d = 0 \text{ vs. } H_1: \mu_d \neq 0$$

$$\text{test statistics} = \frac{\bar{x} - \mu_d}{\frac{s}{\sqrt{n}}}$$

$$\text{critical value } 1-\alpha, 1-\frac{\alpha}{2}$$

$$df = n-1$$

$$H_0: p_1 = p_2 \text{ vs. } H_1: p_1 \neq p_2$$

$$\text{test statistic} = \frac{|\hat{p}_1 - \hat{p}_2| - \left(\frac{1}{2n_1} + \frac{1}{2n_2}\right)}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$$

$$\text{critical value} = 1 - \frac{\alpha}{2}$$

contingency table :-

$$2 \times 2 \Rightarrow \chi^2 = \frac{(O-E)^2}{E} + \dots$$

$$\text{critical value } 1, 1-\alpha$$

$$df = 1$$

$$R \times C \Rightarrow \chi^2 = \frac{(O-E)^2}{E} + \dots$$

$$\text{critical value} = R-1, C-1, 1-\alpha$$

$$df = (R-1) \times (C-1)$$

$$\text{Goodness of Fit} \Rightarrow \frac{(O-E)^2}{E} + \dots$$

$$\text{critical value} = \chi^2(g-k-1), 1-\alpha$$

$$df = g-k-1$$

$$H_0: \mu_1 = \mu_2 \text{ vs. } H_1: \mu_1 \neq \mu_2$$

$$\text{test statistic} = \frac{\bar{y}_1 - \bar{y}_2}{\sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

$$\text{critical value } 1-\alpha, 1-\frac{\alpha}{2}$$

$$df = n_1 + n_2 - 2$$

$$H_0: \rho = 0 \text{ vs. } H_1: \rho \neq 0$$

$$\text{test statistic} = \frac{r\sqrt{n-2}}{\sqrt{1-r^2}}$$

$$\text{critical value} = 1 - \frac{\alpha}{2}$$

$$df = n-2$$

$$H_0: p = p_0 \text{ vs. } H_1: p \neq p_0$$

$$z = \frac{1}{2} \ln\left(\frac{1+r}{1-r}\right)$$

$$z_0 = \frac{1}{2} \ln\left(\frac{1+p}{1-p}\right)$$

$$\text{variance} = \frac{1}{n-3}$$

$$\lambda = (z - z_0) \sqrt{n-3}$$

$$\text{critical value} = 1 - \frac{\alpha}{2}$$

Confidence Interval

* Population mean μ

$$CI = \bar{x} \pm z_{1-\frac{\alpha}{2}} \times \frac{s}{\sqrt{n}}$$
$$= \bar{x} \pm t_{(n-1, 1-\frac{\alpha}{2})} \times \frac{s}{\sqrt{n}}$$

* Population proportion p

$$CI = \hat{p} \pm z_{1-\frac{\alpha}{2}} \sqrt{\frac{\hat{p}q}{n}}$$

* Paired μ_d

$$CI = \bar{d} \pm t_{(n-1, 1-\frac{\alpha}{2})} \frac{sd}{\sqrt{n}}$$

→ mean different ($\mu_1 - \mu_2$)

$$CI = \bar{x}_1 - \bar{x}_2 \pm t_{(n_1+n_2-2, 1-\frac{\alpha}{2})} s \sqrt{\frac{1}{n_1} + \frac{1}{n_2}} \quad (s)$$

$$CI = \bar{y}_1 - \bar{y}_2 \pm t_{(n-k, 1-\frac{\alpha}{2})} s \sqrt{\frac{1}{n_1} + \frac{1}{n_2}} \quad (r_2)$$

* correlation coefficient (ρ)

$$r = \frac{e^{2z_1} - 1}{e^{2z_1} + 1}$$

$$z_1 = \frac{z - z(1-\frac{\alpha}{2})}{\sqrt{n-3}}$$

Interval \pm standard deviation \times $\frac{1}{\sqrt{n}}$

P-Value

two-tailed \rightarrow 2x small area

one tail \rightarrow small area

absolute value (|t|) \Rightarrow small value

+

goodness of fit

+

F-distribution.